

ELECTROCHEMICAL IMPEDANCE SPECTROSCOPY

ADVANCEMENTS AND APPLICATIONS



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INSTITUTE OF ELECTROCHEMISTRY AND
ACADEMICIAN EVGENI BUDEVSKI ENERGY SYSTEMS



ABOUT THE INSTITUTE





PROFILE

Established in 1967 as an Institute for Fundamental and Applied Research and Development in the Field of Electrochemistry and Electrochemical Power Sources.

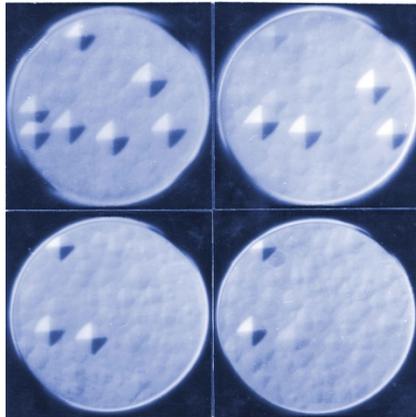
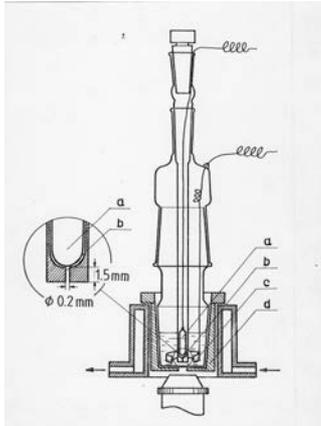
➤ Scientific & Industrial Background

- Electric cars (fork-lift) for industrial applications – 1st place
- Lead/Acid Batteries – 4th in the world
- First dislocation free single crystal



SCIENTIFIC BACKGROUND

- 1936 - two-dimensional theory of crystal growth of **Stranski-Kaischew**
- 1965 - the first dislocation free single crystal
- 16 months later – **Texas Instruments (USA)** – first dislocation free Si crystal



• Silver single crystal [100] face





PROFILE

STAFF ~ 100 people

Academic:

2 Academicians

6 Professors

5 Emeritus Professors

4 Honorable Professors

12 Assoc. Professors

24 Research fellows (15 with Ph. D.)

20 Technical research staff
(14 with Masters degree)

12 Ph. D. Students

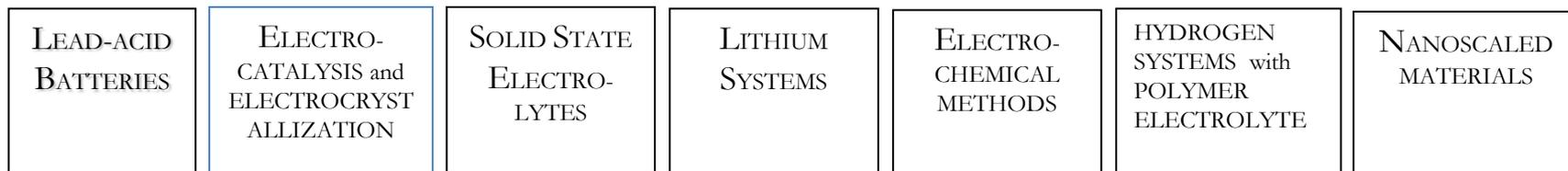
2 THEMATIC PLATFORMS:
BATTERIES + FUEL CELLS





8 SCIENTIFIC DEPARTMENTS in 2 JOINED THEMATIC PLATFORMS:

BATTERIES & FUEL CELLS AND HYDROGEN



TECHNICAL LABORATORIES AND GROUPS

•LABORATORY FOR MATERIALS TESTING

•MECHANICAL WORKSHOP

•ELECTRIC WORKSHOP

SEM/ED

Hg-porosimeter

X-ray diffractometer

BET surface analyzer

Thermo/analytical equipment

+ access to BAS Equipment (about 200 instruments)

•Administration and Accounting

2015 - 25 Projects and Contracts (National and International)





✓ **European Commission** : FP 3 - 7 (14 projects); NATO; IUPAC;

2003 - *Centre of Excellence* on Portable and Emergency Energy Sources

FP 7 – 5 projects

✓ **Companies:** ILZRO (TRP – USA); ALABC (USA) & EALABC (Europe), Gould (USA), US Army; ChemTek GmbH (D); Fraunhofer (D); Lucas (UK); Oerlicon (Sw); Bohemia (Cz), ENEL..... *Segasa (Sp); Varta (D)*,

✓ **Academic:** CNRS (Fr); Royal Society (UK); CNR (It); JRC- Petten; Polish, Rumanian Academies of Sciences; Many Universities (Greece, UK, Germany); ERASMUS



Scientific & business partners :

(for the last 5 years)

more than 150 from

~ 30 countries





JOINT THEMATIC PLATFORMS

➤ BATTERIES



➤ FUEL CELLS & HYDROGEN

90^{ths} of the 20th century



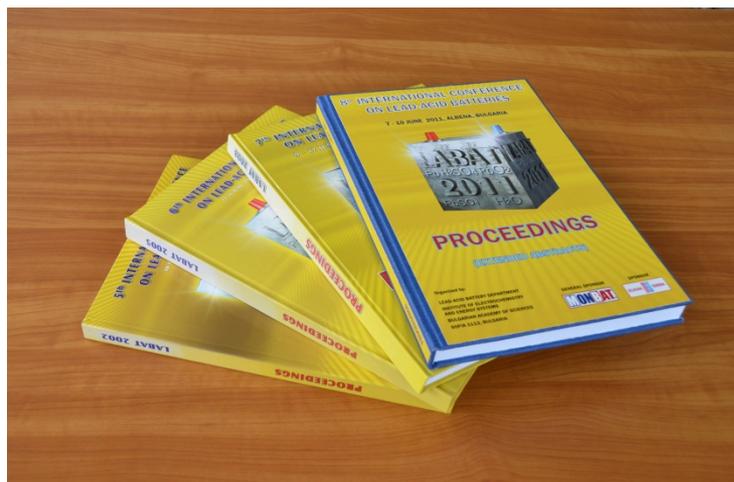
Scientific Strategy: “TRADITION AND INNOVATIONS”



➤ BATTERIES

✓lead-acid batteries

- International research support - contracts with the largest international companies
 - LABAT
 - Optimization for RES and electric cars
- NEW TRENDS





➤ BATTERIES

✓ Metal (Zn, Mg)/air batteries (3 generations)

- primary
- mechanically rechargeable
- Rechargeable – recently

Bulgarian Himalayan expeditions



World record

Salt Lake (USA) - 1997



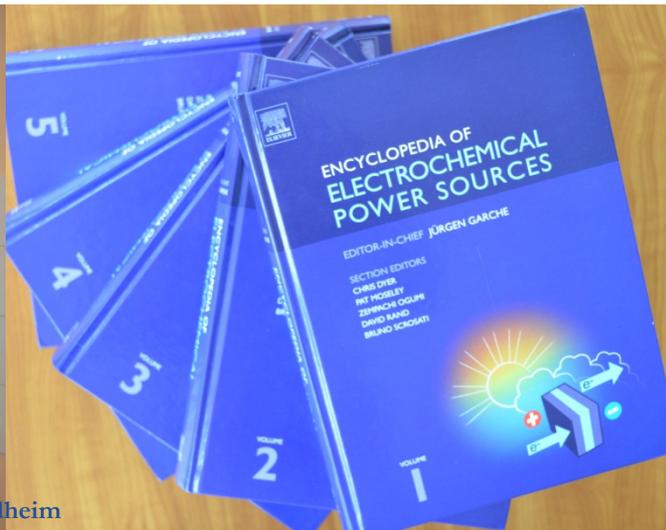
sea signalization
buoys (Baltic sea)





➤ BATTERIES

- ✓ **Li and Li-ion batteries** (4th country in the world in production of primary Li-SO₂)
 - new designs (Li/air)
 - nano- nano-scaled composites (metal-carbon, silicon-carbon)
- ✓ **Ni-Zn rechargeable** – project with Bohemia
- ✓ **Electrochemical methods for batteries and fuel cells testing** - diagnostic of batteries r accumulation from RES (> 500 V) – project with ENEL

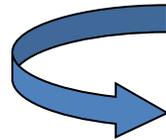




➤ Fuel Cells & Hydrogen – 90ths of the 20th century

Renewable Energy Sources (Energy Efficiency) - NOW

- ✓ fuel cells – PEM, SOFC
- ✓ hydrogen production
- ✓ hydrogen storage
- ✓ electrochemical methods for fuel cells testing (impedance spectroscopy)



4 FP 7 contracts:

1 in FCH JU

1 in Energy;

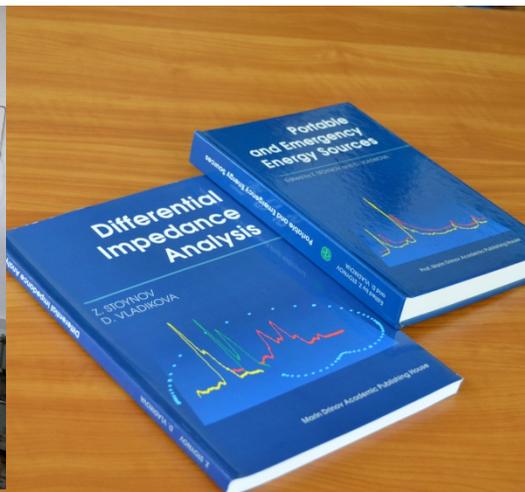
2 in Marie Curie





✓ Electrochemical methods for batteries and fuel cells testing (impedance spectroscopy)

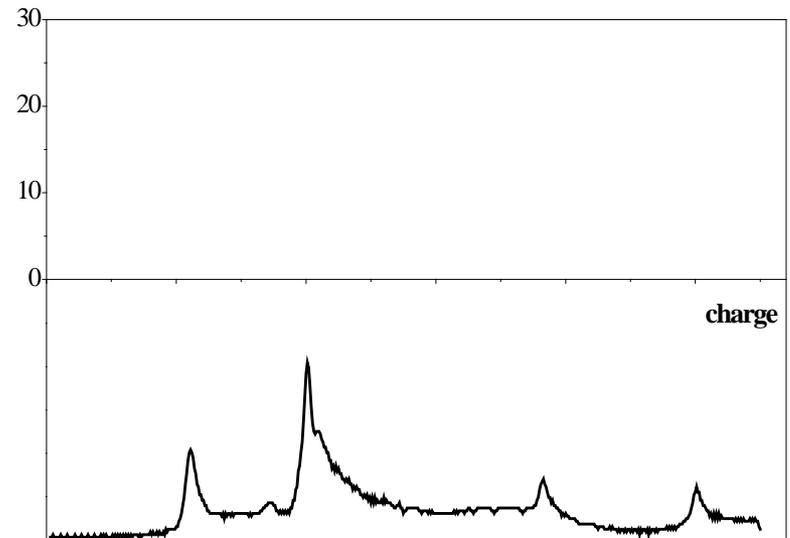
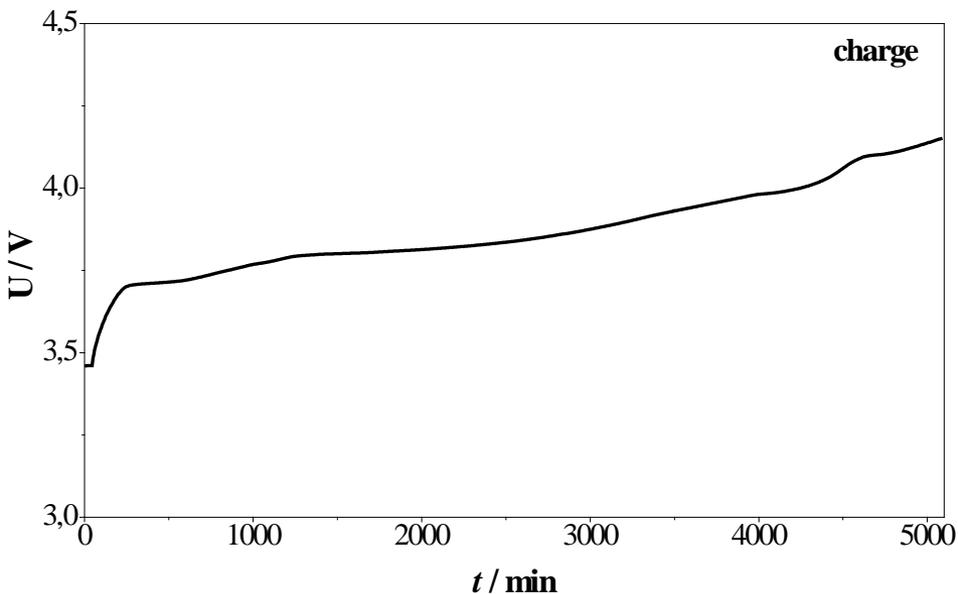
- Non-standard equipment
- Innovative electrochemical methods for characterization and testing of functional materials
 - Nonstationary impedance (Mitsubishi (*Li-batteries*),
 - Differential Impedance Analysis (data analysis without preliminary working hypothesis)





✓ Electrochemical methods for batteries and fuel cells testing (impedance spectroscopy)

- Innovative electrochemical methods for characterization and testing of functional materials
 - Differential Coulometry Spectroscopy – for precise characterization and testing of batteries

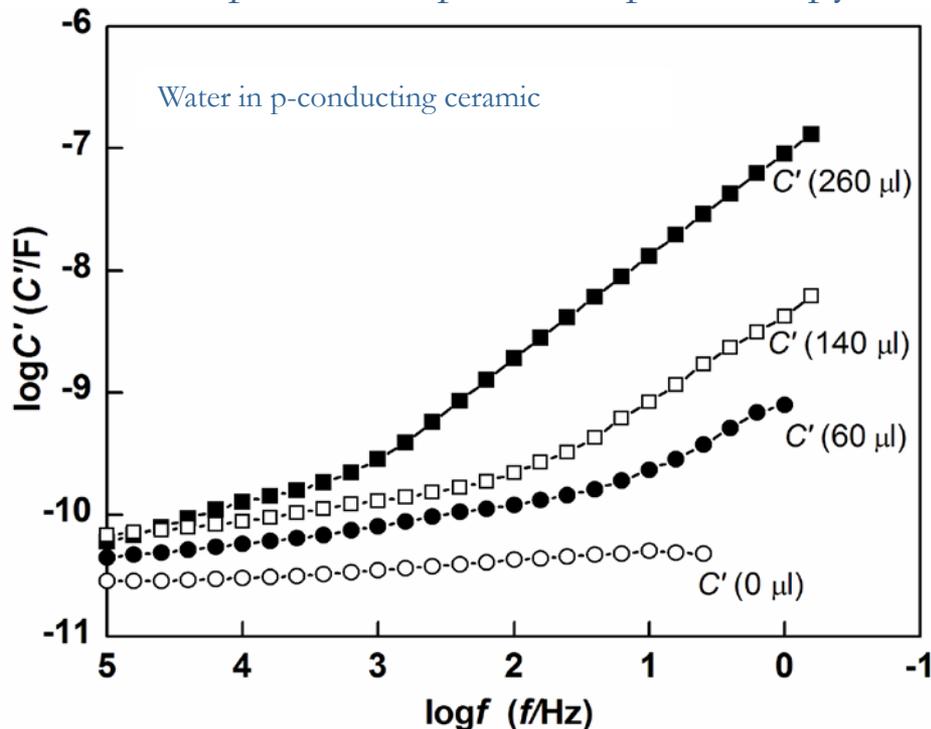




✓ Electrochemical methods for batteries and fuel cells testing (impedance spectroscopy)

- Innovative electrochemical methods for characterization and testing of functional materials

○ Capacitive Impedance Spectroscopy



Last years:

- Impedance based approaches for characterization and testing of fuel cells



Testing Units (can be used for impedance)



0.1 A/0.01 A; 5 V

Star1

0.1 A C/D
16 channels

1



5 A; 2V

Star2

5 A Dch
16 channels

2



200A; 24V

Star3

100/200 A C/D
Single
channel

3



1000A; 12/6V *Star6*

1000 A
12 V
Single
Channel

6



BASICS OF IMPEDANCE SPECTROSCOPY – e-learning

1. Why Impedance

2. What is impedance

3. Impedance measurements

- Basic Working Hypotheses

4. Presentation of the experimental data

5. Interpretation of the measured data (data analysis)

- Impedance elements
- Simple models
- Identification



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Why Impedance - Advantages

➤ From scientific point of view:

- **UNIQUE ADVANTAGE:** to separate the kinetics of the different steps involved in the total process under investigation
- Assessment of processes with different velocity
- Easy performance of experiments with accessible digital instruments
- Maturity in the software exploitation
- Easy performance of virtual impedance data analysis (e-data analysis)

➤ From applied point of view:

Covers wide range of objects:

- Batteries
- Semiconductors
- Fuel cells
- Nano-materials
- Biosensors
- Ceramics
- Biological objects
- Materials testing
- Corrosion
- Crystallization





**Internat. Symp. on EIS
(every 3 years)**

Ist - 1989 - FRANCE

IIInd - 1992 - USA

IIIrd - 1995 - BELGIUM

IVth - 1998 - BRAZIL

Vth - 2001 - ITALY

VIth - 2004 - USA

VIIth - 2007 - FRANCE

VIIIth - 2010 - PORTUGAL

IXth - 2013 - JAPAN

**Internat. Mycrosymp
on EIA
(every 3 years)**

Ist - 1987 - RUSSIA

IIInd - 1990 - BULGARIA

IIIrd - 1993 - BULGARIA

IVth - 1996 - POLAND

Vth - 1999 - HUNGARY

VIth - 2002 - CZECHIA

VIIth - 2006 - CZECHIA

VIIIth - 2008 - CHECHIA

IXth - 2011 - CROATIA

Xth - 2014 - BULGARIA

Xith - 2017 - ITALY

2001 *Established*

**European Internet
Centre
For Impedance
Spectroscopy (EICIS)**

base organization

IEES - BAS

**Online Journal
*Impedance
Contributions Online***

Online consultations





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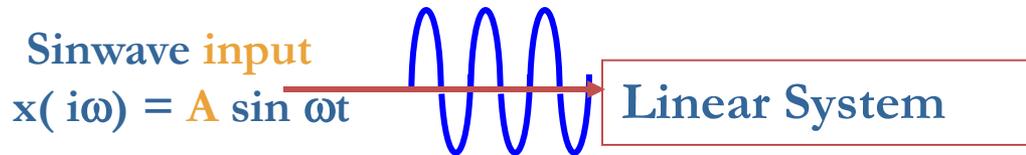


- The Electrochemical Impedance Spectroscopy is based on the classical method of the **TRANSFER FUNCTION (TF)**

Linear System



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Principle:

- If the system under investigation is **LINEAR (LS)**,

sin-wave input $x(i\omega)$ perturbation \longrightarrow $y(i\omega)$ output measurement

The response $y(i\omega)$ is also sin wave with the **same frequency** and **different amplitude and phase**;

- The ratio **output / input signal** determines the complex **transfer coefficient** for the corresponding frequency:

$$k(i\omega) = y(i\omega) / x(i\omega)$$

Complex number (Re; Im)
Depends on ω and the object's properties





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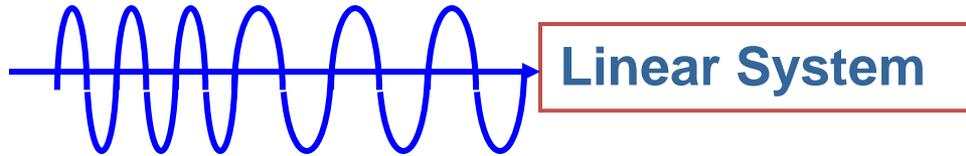
$$k(i\omega) = y(i\omega) / x(i\omega)$$

↙ ↘ Complex number (Re; Im)
Depends on ω and the object's properties





Linear System



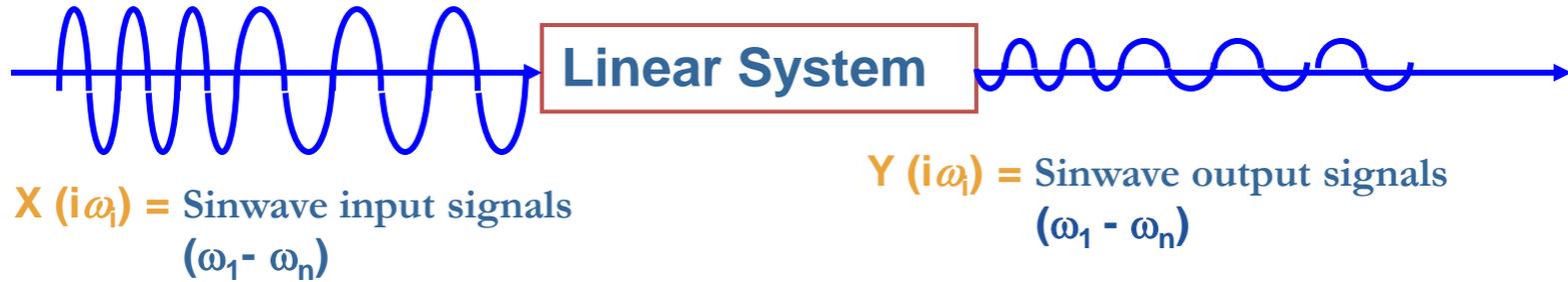
$X(i\omega)$ = Sinwave input signals
($\omega_1 - \omega_n$)

$$H(i\omega) = Y(i\omega) / X(i\omega)$$

is the **T**ransfer **F**unction

TF describes the frequency dependence of the transfer coefficient $k(\omega)$

- The transfer from the time-domain to the frequency domain is performed by **LAPLAS** transform. For **steady state** linear systems it is replaced by **FOURIER** transform.



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TF describes the frequency dependence of the transfer coefficient $k(\omega)$

- The transfer from the time-domain to the frequency domain is performed by **LAPLAS** transform. For **steady state** linear systems it is replaced by **FOURIER** transform.



➤ TF is impedance $\longrightarrow H(i\omega_i) = Z(i\omega_i)$

input signal - current (I)

output signal - voltage (U)

➤ TF is admittance $\longrightarrow H(i\omega_i) = Y(i\omega_i) = Z^{-1}(i\omega_i)$

input signal - voltage (U)

output signal is current (I)

➤ When the frequency range ($\omega_1 - \omega_n$) is ω large and covers all the properties of the system, the system is **observable**, otherwise it is **partially observable**.

Conclusion:

The Transfer Function $H(i\omega_i)$ describes totally a linear, steady-state and observable system.



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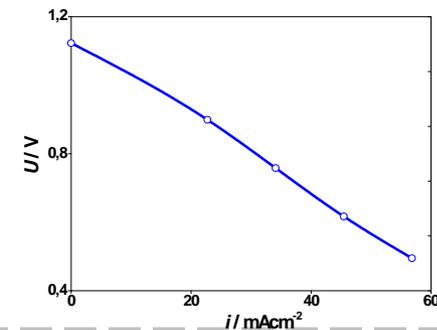


Impedance as a Transfer Function $H(i\omega)$ describes totally a linear, steady-state and observable system.

➤ Electrochemical systems:

large
non-linear →
non-steady state
semi-irreversible
distributed parameters
mass- and energy transfer take place

SOFC are quasi-linear



The TF approach needs a number of simplifications and assumptions, generalized in

BASIC WORKING HYPOTHESES

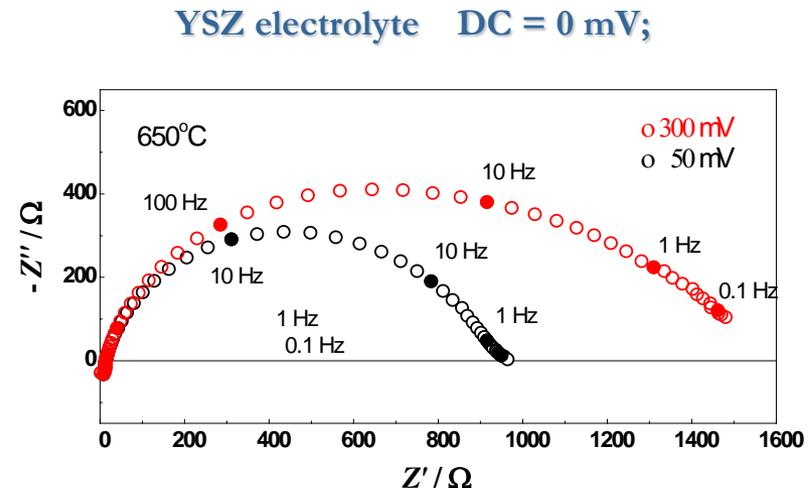
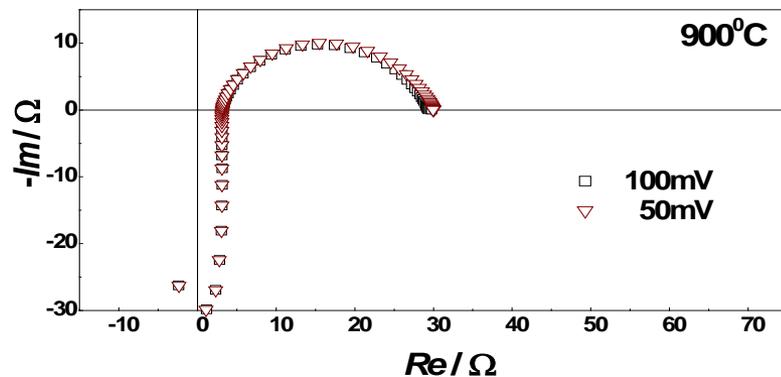


➤ Working hypotheses from system analysis point of view

✓ **Linearity:** the input perturbation signal should be small enough to keep the state of the investigated system unchanged.

The requirement for a small signal covers the potential, the current, as well as the quantity of electricity for half a period (very important at low frequencies!).

Experimental verification: Consecutive impedance measurements in the full frequency range with decreasing amplitude and analysis of the weighted differences.

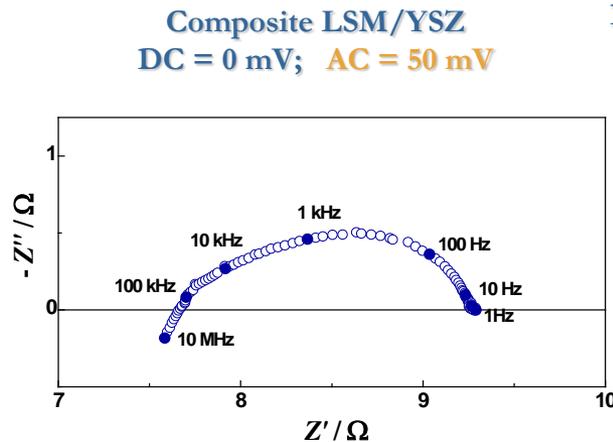
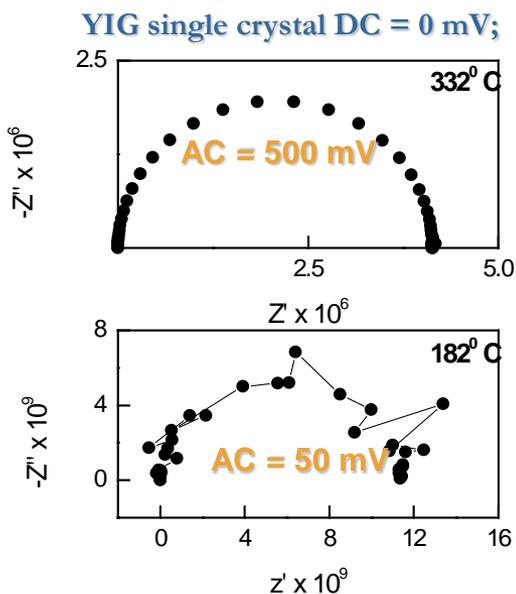




➤ Working hypotheses from system analysis point of view

✓ **Linearity:** the input perturbation signal should be small enough to keep the state of the investigated system unchanged.

Small signal: depends on the investigated system



Dislocation free Ag single crystal
DC = 5 mV;
AC = 50 mV

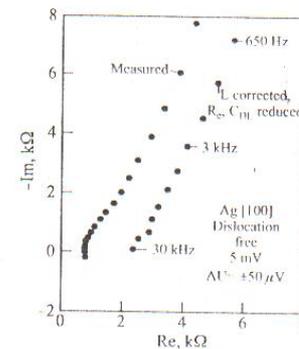
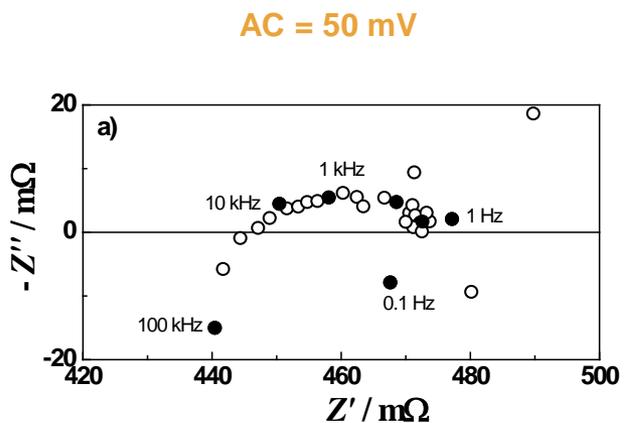
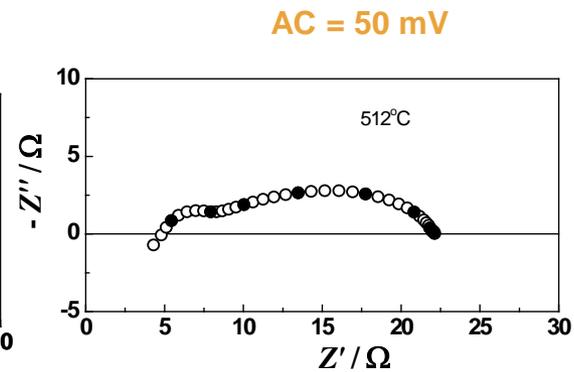
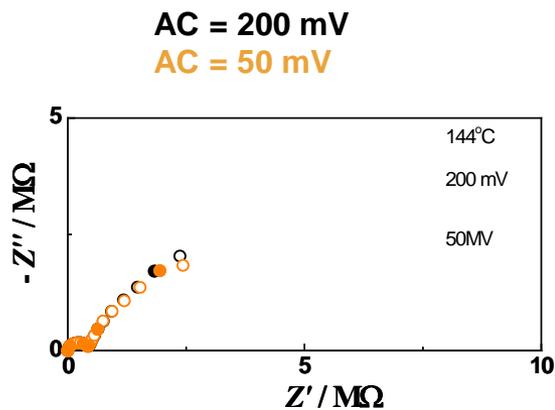
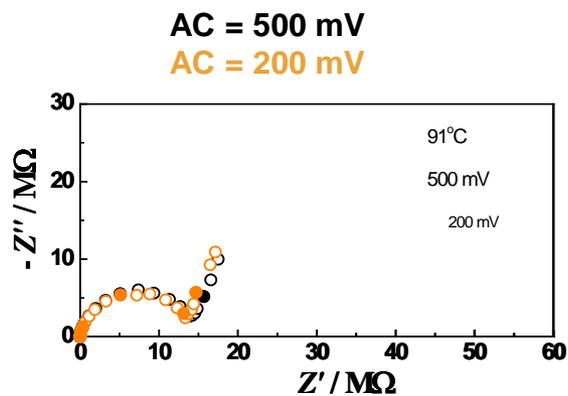


Fig. 3. Impedance plots

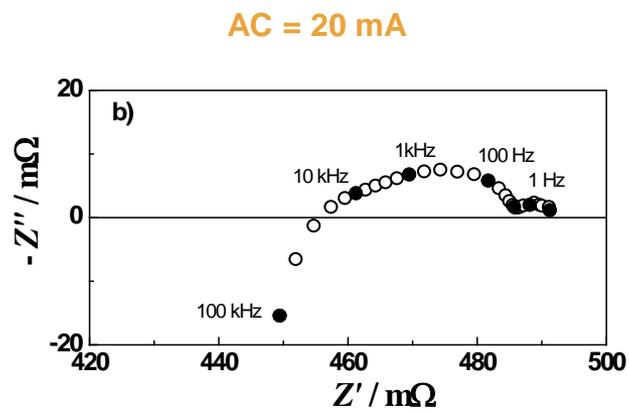


Small signal : depends on the investigated system

LSCF/YDC/LSCF
DC = 0 mV



719°C



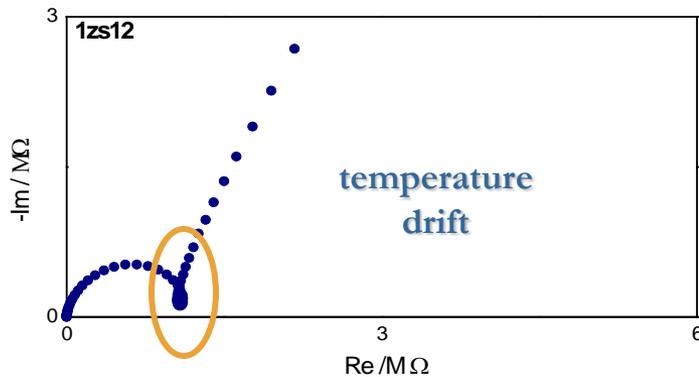


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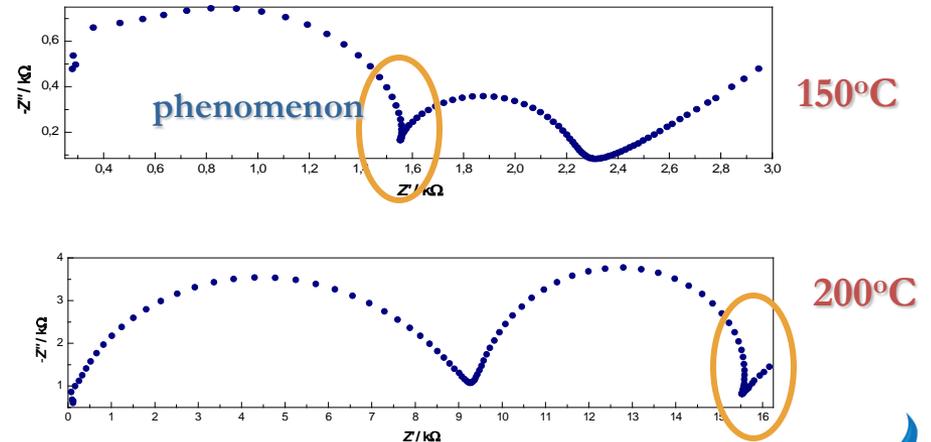
✓ **Single input, single output:**

achieved if the rest of the parameters (temperature, concentration, d.c. signal, pH etc.) are kept constant by passive or active conditioning.

Oxygen conducting ceramic



Proton-conducting ceramic

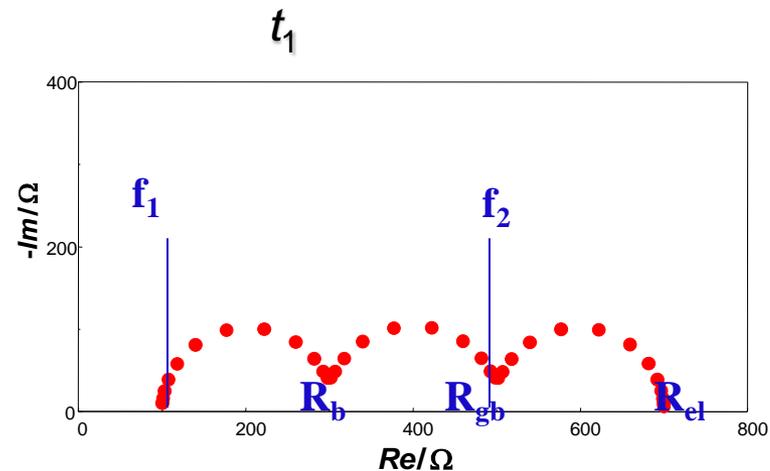
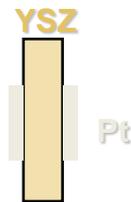




➤ Working hypotheses from system analysis point of view

✓ **Observability:**

All the phenomena under study can be observed in the measured frequency range.

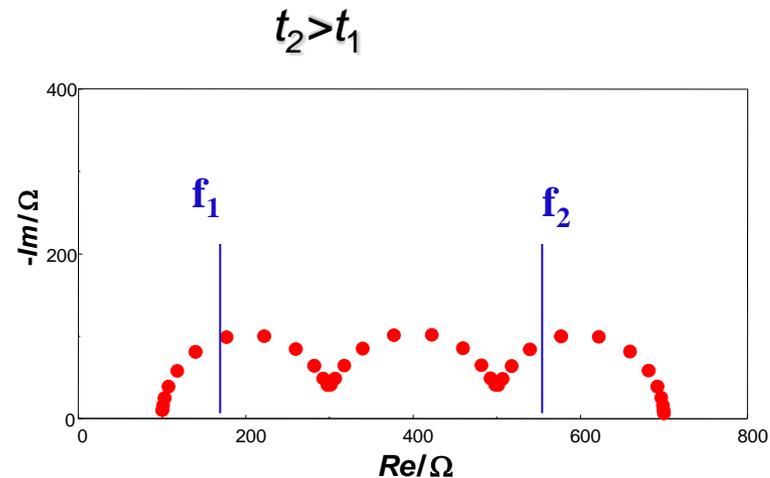
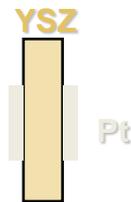




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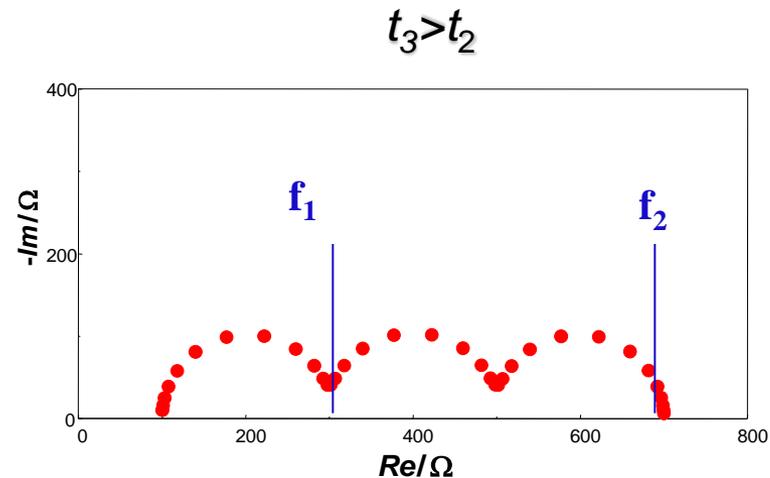
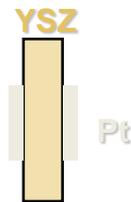


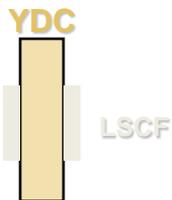


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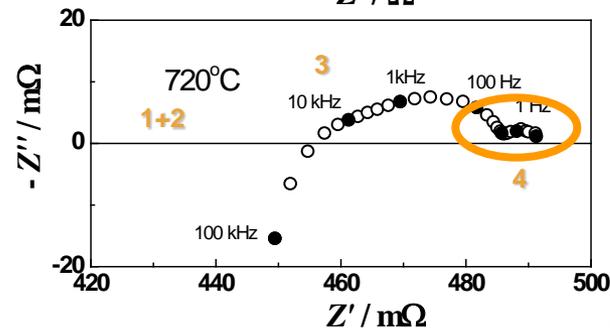
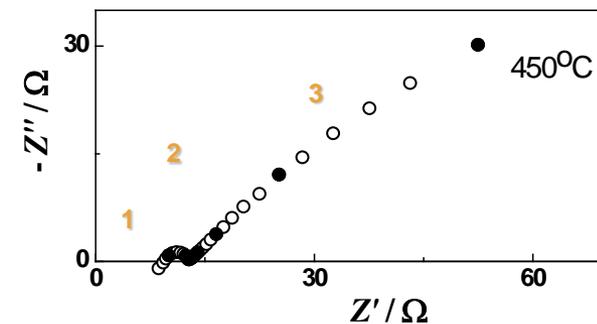
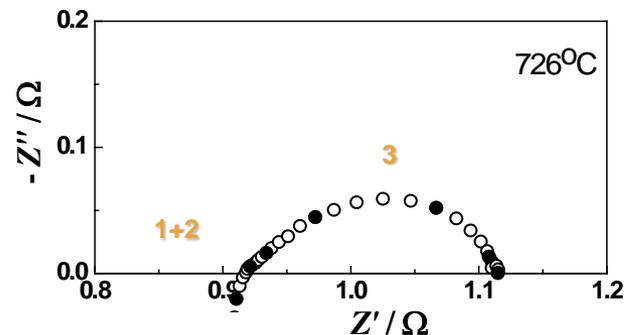
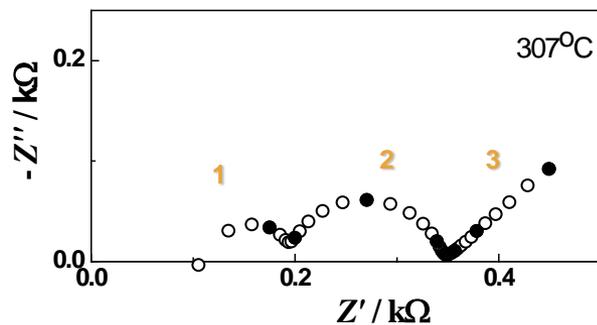
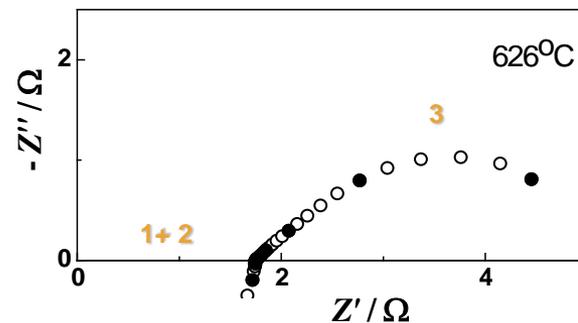
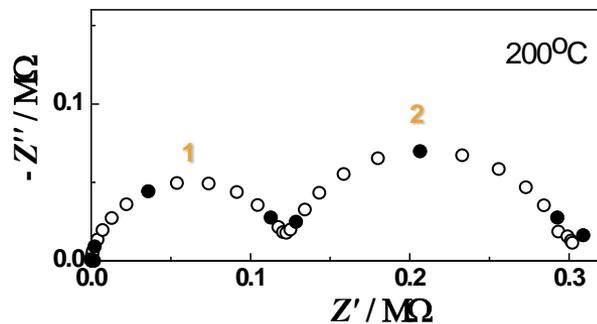
All the phenomena under study can be observed in the measured frequency range.





f_1 f_2
10 MHz 0,01 Hz

Both electrolyte (YDC) and electrode (LSCF) behavior become observable

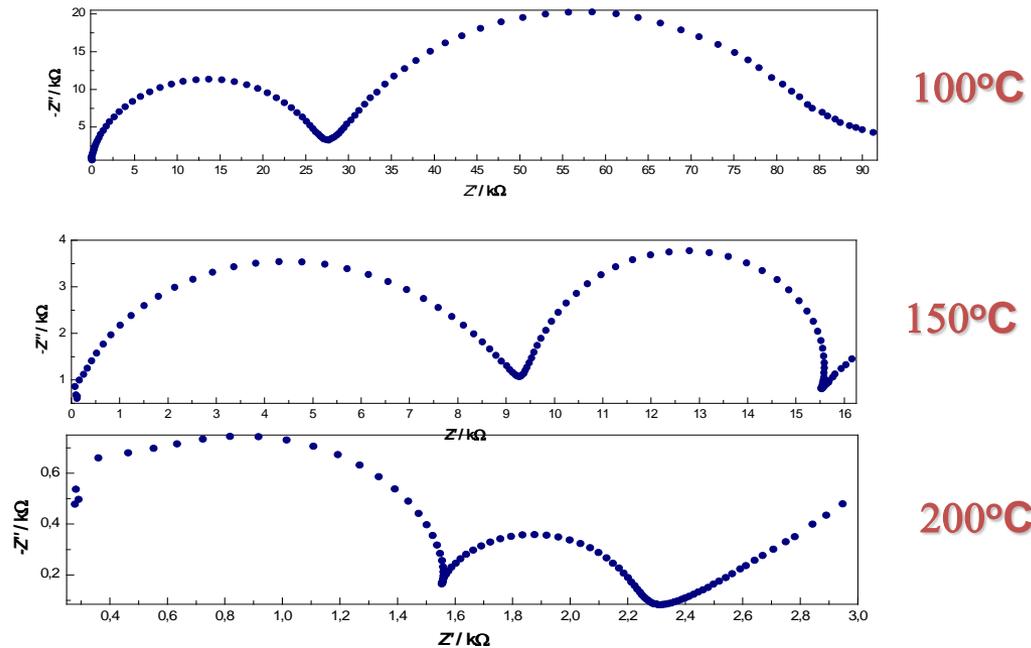




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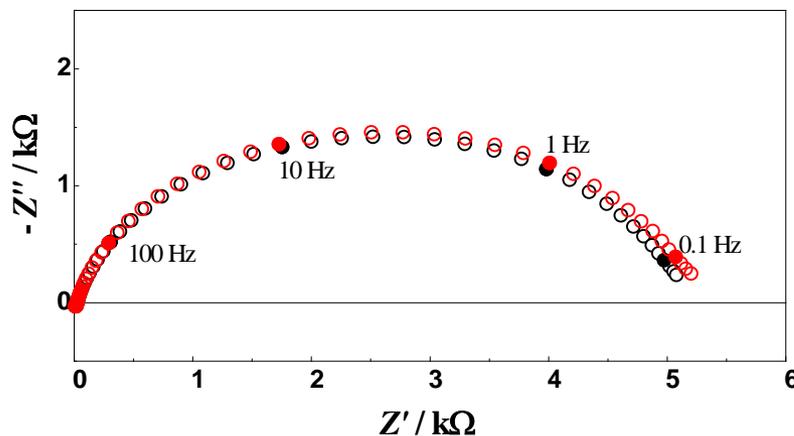


✓ **Lack of memory effects:**

the investigated system does not “remember” the history of the experiment. That means that the result does not depend on the order of the measurements.

Experimental verification: measurements from high to low and then from low to high frequencies, + analysis of the weighted differences.

Recommendation: down-scanning



YSZ: 650° C

◦ Up (from high to low frequencies)

◦ Down (from low to high frequencies)



✓ For Systems that:

OBEY the working hypotheses

CAUSAL (all the changes are caused by the perturbation signal)

Hilbert Transform:

full description of the object with only with Re (or Im)

Experimental application: Kramers-Kronig Transform (KK)

$Im \rightarrow Re$ or $Re \rightarrow Im$

KK is valid ONLY for a class of electrochemical objects





- Working hypotheses from electrochemical point of view
 - ✓ **Additiveness** of the Faradaic current and the charging current of the double layer
 - ✓ **Electrical neutrality of the electrolyte** – the total density of the charges in every point of the solution is zero
 - ✓ **Lack of convection and migration** – i.e. there are no changes in the local concentration of the electrolyte
 - ✓ **Lack of lateral mass and charge fluxes** at the electrode surface.



➤ New Trends in the Electrochemical Impedance

✓ **AIM:** To overcome the restrictions of the working hypotheses:

☺ NON -LINEAR Impedance

☺ NON-STATIONARY Impedance

☺ MULTI-TRANSFER FUNCTION ANALYSIS –
single input and multiple outputs



➤ Working hypotheses - Conclusions

✓ ONLY correct experimental conditions ensure

- ☺ accuracy
- ☺ reliability of the measured impedance data

✓ Correct experimental conditions depend on:

- ☺ construction of the experimental cell + object configuration
- ☺ measurement setup
- ☺ correct combination of parameters and conditions (*small signal, scan from high to low frequencies, well defined working point – constant values of all the parameters*)





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➤ Impedance monitoring

$$Z(i\omega_i) = Y(i\omega_i) / X(i\omega_i) = U(i\omega_i) / I(i\omega_i)$$

complex number

3D data set $Z(Re_i, Im_i, \omega_i)$

✓ Cartesian coordinates:

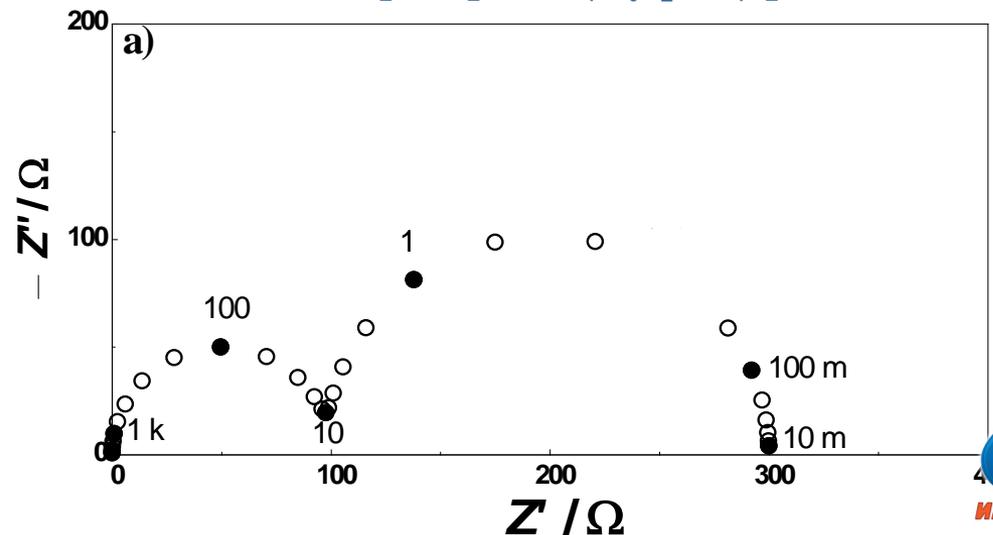
$$Z(i\omega_i) = Re_i + iIm_i; \quad i = (-1)^{1/2}; \quad i = 1, 2, \dots, n - \text{frequency range}$$

Coordinates: $x_i = Re$; $y_i = -Im$

Nd – frequency density; 3-5 for screening; 10-15 for precise measurements;

Data pre-processing: data quality improvement - correction of erroneous data

Complex plane (Nyquist) plot





✓ **Polar coordinates:** $Z(i\omega_i) = |Z| e^{j\phi_i}$ - Bode Plots

$|Z| = (Re_i^2 + Im_i^2)^{1/2}$ - modulus ; $\phi_i = \text{Arc tan } (Im_i/Re_i)$ - phase

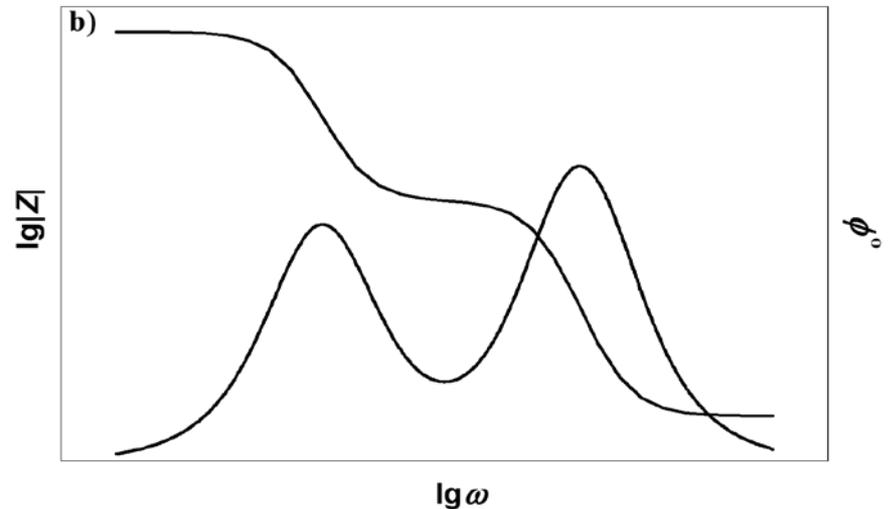
Recalculated 3D set of data:

$D3 [\omega_i, |Z|_i, \phi_i]$; $i = 1, 2, ..n$

Coordinates:

$$x_i = \lg \omega_i; \quad y1_i = |Z|_i \\ y2_i = \phi_i$$

Bode Plots





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From one side the impedance (or admittance) functions contain **all the information for the investigated system** (if the working hypotheses are fulfilled at the selected working point).

From another side this information has to be extracted from the data, i.e. the **data analysis is an identification procedure**.

Advantage: The electrochemical impedance has the unique possibility to separate the kinetics of the different steps involved in the total process under investigation, because as a transfer function it is a local, linear and full description of the system under study. A number of processes are taking place, caused by the perturbation signal. The impedance, however, does not measure them, i.e. it is not a physical reality, but information property of the object.

Disadvantage: Since impedance is not a physical reality, the interpretation of the experimental data is based on the construction of a **WORKING MODEL**, following a preliminary working hypothesis, which should be identified. This introduces a subjective component in the analysis.





Impedance (as a Transfer Function) gives a **local, linear an full description** of the system under study.

➤ **Data analysis** – construction of a model by identification procedure.

✓ **Theoretical (classical) identification approach**

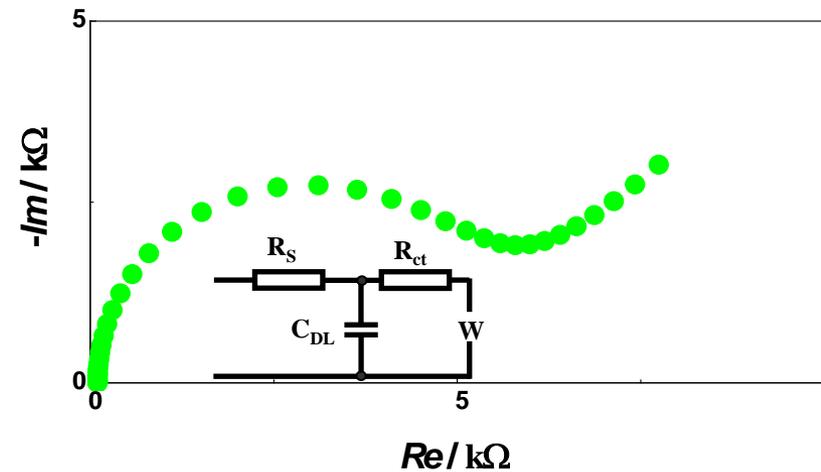
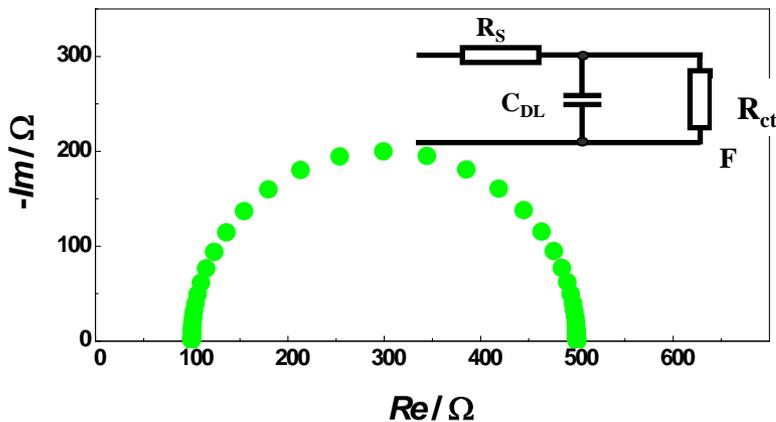
- construction of a working model(s), following a preliminary working hypothesis
- verification of the model by parametric identification

✓ **Structural identification approach**

- no need of a preliminary working hypothesis
- extracts the model structure + parameters from the experimental data (DIA)



- Model representation by equivalent circuits - construction of different elements connected under given laws



- ✓ The electrical circuit has a response identical to that obtained from the measurement of the investigated system.
- ✓ Every element describes part of the physical processes taking place
- ✓ If the model is not formal, the values of its elements could give a significant contribution to the physical understanding of the investigated system.



1. Why Impedance
2. What is impedance
3. Impedance measurements
 - Basic Working Hypotheses
4. Presentation of the experimental data
5. Interpretation of the measured data (data analysis)
 - Impedance elements
 - Simple models
 - Identification



- **Lumped (electrical) elements** – describe homogeneous systems (electrical elements)
 - ✓ resistance R ;
 - ✓ capacitance C ;
 - ✓ inductance L .
- **Frequency dependent (electrochemical) elements** – describe frequency inhomogeneity (electrochemical processes)



➤ Resistance R

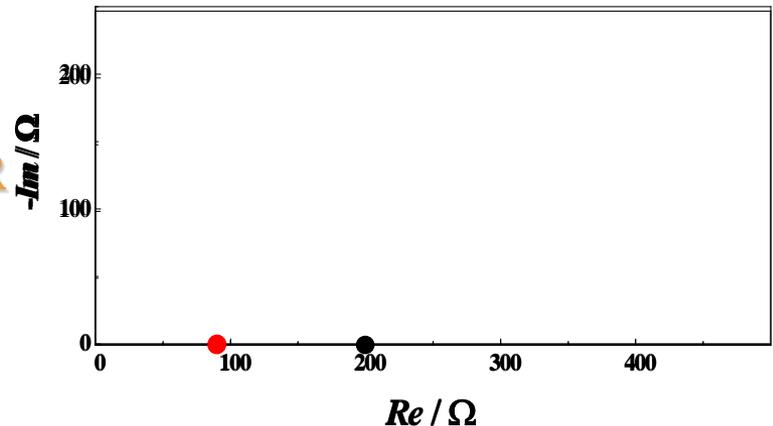
- ✓ In the time (t) domain – follows Ohm's Law: $U_R = R \cdot I$
Dimensions: ohm (Ω) = $\text{VA}^{-1} = \text{m}^2\text{kgA}^{-2}\text{s}^{-3}$
- ✓ In the frequency (ω) domain: $Z_R(i\omega) = R$
only real part ($Re = R; Im = 0$)

✓ Physical meaning: - description of:

energy losses;
dissipation of energy;
potential barrier;
electronic conductivity
conductivity of very fast carriers



R



- ✓ Electrolyte resistance - $Z_s(i\omega) = R_s$
for water based electrolytes



➤ Inductance L

- ✓ In the time (t) domain
Dimensions: $H = \Omega s$

$$U_L = L \frac{di(t)}{dt}$$

- ✓ In the frequency (ω) domain:
only imaginary part ($Re = 0$)
 90° phase shift; $Z \uparrow$; $\omega \uparrow$

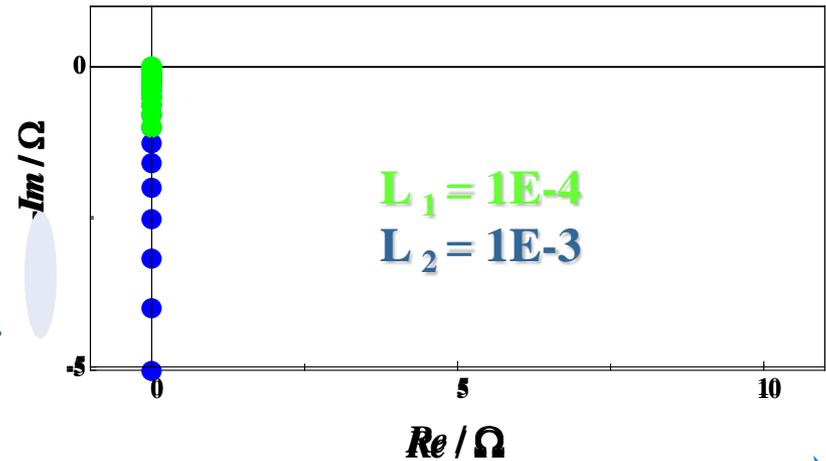
$$Z_L(i\omega) = i\omega L$$


- ✓ Physical meaning: - modeling of:

self inductance of the connecting cables, the measuring cell and investigated objects

self inductance of current flow or of charge carriers movement;

- ✓ Represents accumulation of magnetic energy





- Frequency dependent (electrochemical) elements – describe frequency dependent behaviour



➤ **Warburg element (1896) W** - describes linear semi-infinite diffusion, which obeys the second Fick's law:

✓ In the time (t) domain
Dimensions: $\Omega m^2 s^{1/2}$

✓ In the frequency (ω) domain:
 $Re = Im$ – phase shift = 45°

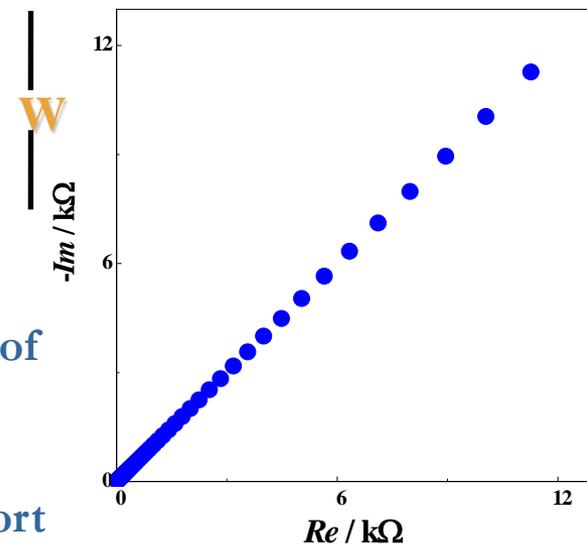
✓ Remark:

the sin wave does not reach the end of the diffusion layer.

Warburg impedance is a one port element – no introduction of another element after Warburg impedance

$$\partial c / \partial t = D(\partial^2 c / \partial x^2)$$

$$Z_W(i\omega) = \sigma \omega^{-1/2} (1 - i)$$





- **Constant Phase Element (CPE)** – empirical relationship
 - ✓ CPE describes frequency dependent impedance caused by surface roughness or non-uniformly distributed properties of the irregular electrode surface.

$$Z_{\text{CPE}}(i\omega) = A^{-1} (i\omega)^{-n}$$

A – proportional factor [$\Omega\text{m}^{-2}\text{s}^n$];

n – exponential coefficient (CPE exponent)
that describes the phase shift



➤ **Constant Phase Element (CPE)** – empirical relationship

✓ CPE is a generalized element

$n = 0.5 \pm e$ ($0 < e < 0.2$) - diffusion with deviations from the second Fick's law;

$n = 0 \pm e$ - distorted resistance
($n < 0$ is related to inductive energy accumulation);

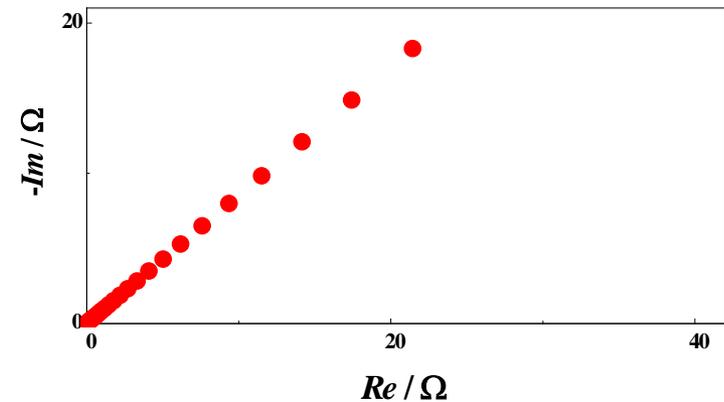
$n = 1 - e$ - distorted capacitance;

$n = -1 + e$ - distorted inductance.

For integer values of n ($n = 1, 0, -1$) – lumped elements C, R and L.

✓ In general CPE is semi-infinite element. It models the impedance of a layer with a thickness bigger than the penetration depth of the perturbation signal.

✓ CPE has only an input with the exception in the cases when $n = 1, 0, -1$.



CPE

$n = 0.45$

$n = 0.2$

$n = 0.8$

$n = 0.9$



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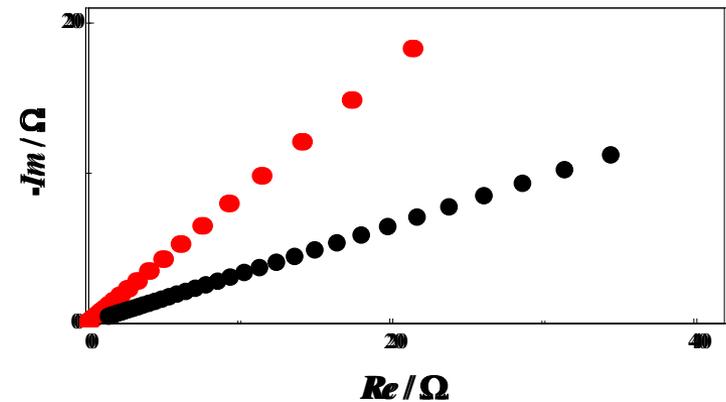
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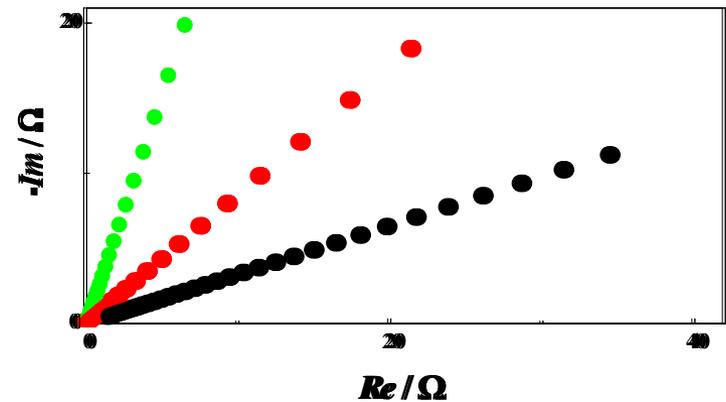
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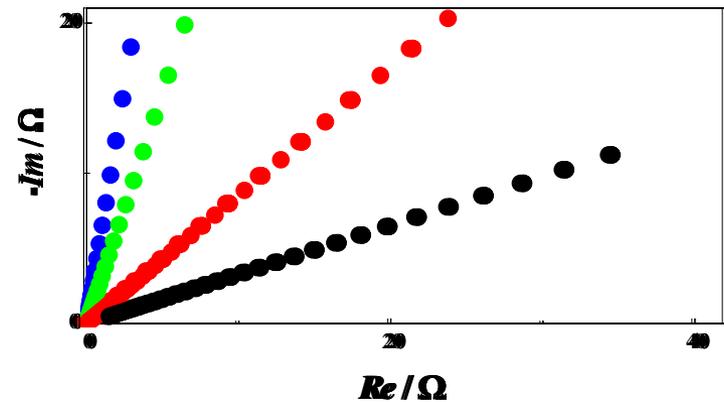
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CPE- Physical Meaning

CPE may have direct **physical meaning** :

the generalized **resistance** $n = 0 - 0.2$ may model conductance of ionic clouds or conductance connected with accumulation of magnetic or electrostatic energy;

the generalized **capacitance** $n = 0.8 - 1$ may model surface roughness of the electrode or distribution of the charge carrier density, i.e. a double layer with complicated structure;

The generalized Warburg $n = 0.4 - 0.6$ may present non-ideal geometry of the diffusion layer; presence of migration or convection; diffusion connected with energy losses or accumulation of charges; constraints of the host matrix to the diffusion of species, unhomogeneous diffusion;

CPE may be also used for **formal** better **modeling** of an external similarity with the measured impedance.





➤ Bounded electrochemical elements

In real systems very often at low frequencies the perturbation signal penetrates to the end of the layer, which behaves as a **layer with a finite thickness**. For more precise modeling of such systems bounded electrochemical elements are introduced.



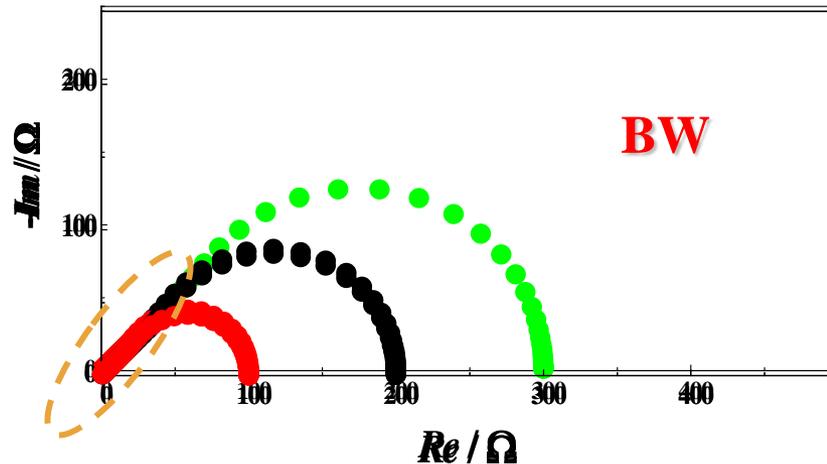
➤ Bounded Warburg (BW)

✓ Bounded Warburg element describes the impedance of a linear diffusion in a homogeneous layer with finite thickness

$$Z_{BW}(i\omega) = \sigma(i\omega)^{-1/2} \operatorname{th}\left(\frac{i\omega R_0^2}{\sigma^2}\right)^{1/2}$$

R_0 is the total resistance [Ω] of the layer at $\omega = 0$

At high frequencies ($\omega \rightarrow \infty$) BW behaves as Warburg element.



$R_0 = 100$
 $R_0 = 200$
 $R_0 = 300$
 $\sigma = 0.01$



➤ **Bounded Constant Phase Element (BCP)** - represents the impedance of a bounded homogeneous layer with CPE behaviour of the conductivity in the elementary volume and a finite conductivity R_0 at d.c. ($\omega \rightarrow 0$)

$$Z_{BCP}(i\omega) = A^{-1}(i\omega)^{-n} \text{th}(R_0 A(i\omega)^n)$$

n and A are the CPE coefficients

$$R_0 = 100$$

$$R_0 = 200$$

$$R_0 = 300$$

$$n = 0.45$$

$$A = 0,01$$

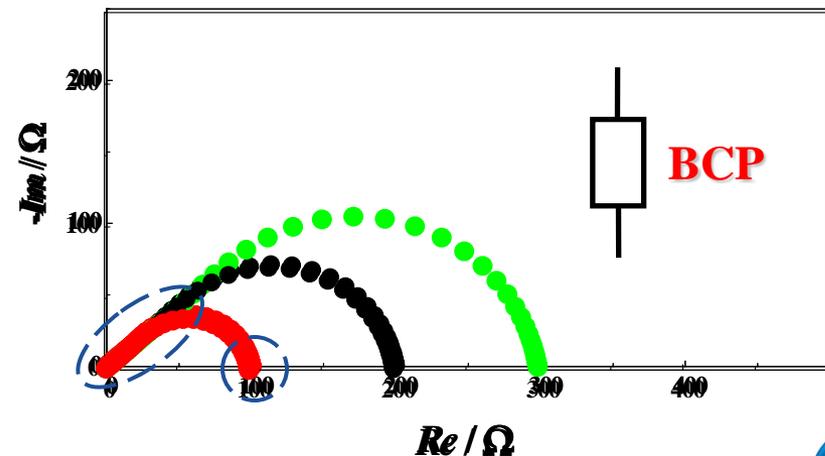
✓ **Properties** – the most generalized element:

for high enough frequencies
tends to the classical CPE

$$Z_{BCP}(\omega \geq \omega_a) = Z_{CPE} + \varepsilon$$

for low frequencies – pure
resistance R_0

$$Z_{BCP}(\omega \leq \omega_b) = R_0 + \varepsilon$$

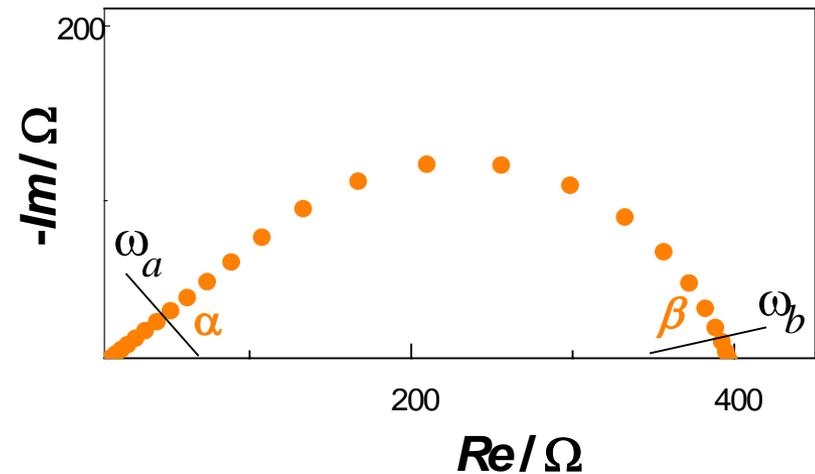




Criterion for verification of BCP:

a and **b** are the angles of the diagram's asymptotes respectively at low and high frequencies.

$$\beta = 2\alpha = (n \pi/2)$$



BCP

$$R_o = 400$$

$$A = 0.01$$

$$n = 0.3$$



➤ **Bounded Constant Phase Element (BCP)**

$$Z_{\text{BCP}}(i\omega) = A^{-1}(i\omega)^{-n} \text{th}(R_0 A(i\omega)^n)$$

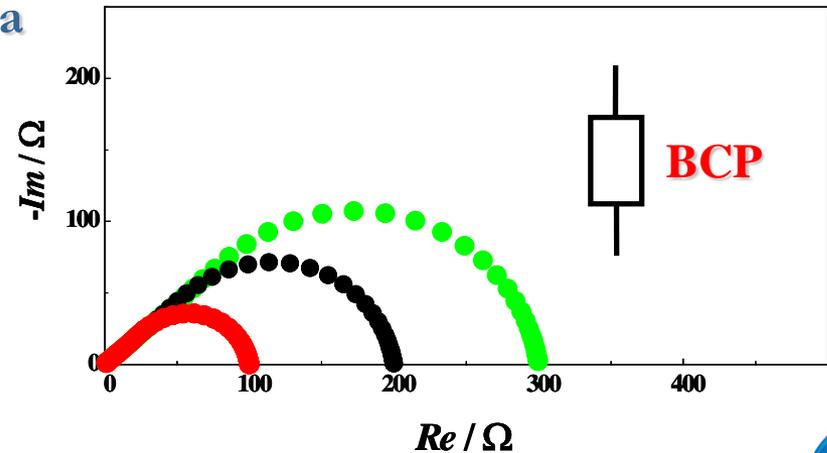
n and A are the CPE coefficients.

✓ **Remark:**

BCP can be applied for $n = 0 - 0.6$ because of the initial assumption that the investigated object is regarded as a conductor.

Obviously at higher values for n the system demonstrates capacitive behaviour.

$R_0 = 100$
 $R_0 = 200$
 $R_0 = 300$
 $n = 0.45$
 $A = 0,01$





Electrical circuit model – construction of different elements connected under given laws

✓ Lumped (electrical) elements

$R \longrightarrow Z_R(i\omega) = R$ energy losses

$L \longrightarrow Z_L(i\omega) = i\omega L$ accumulation of magnetic energy

$C \longrightarrow Z_C(i\omega) = -i(\omega C)^{-1}$ accumulation of mass or charge

✓ Frequency dependent (electrochemical)

$W \longrightarrow Z_W$ semi-infinite diffusion

$BW \longrightarrow Z_{BW}$ bounded diffusion

$CPE \longrightarrow Z_{CPE}$ generalized, semi-infinite

$BCP \longrightarrow Z_{BCP}$ most generalized, bounded





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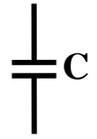


➤ Connections between elements:



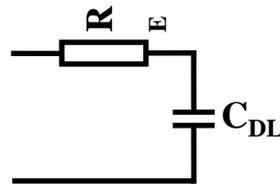
$Z_R(i\omega) = R$

+



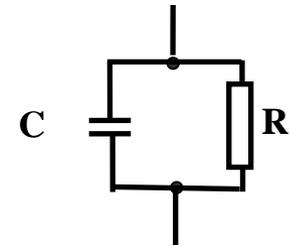
$Z_C(i\omega) = -i(\omega C)^{-1}$

Series
connection



$$Z_{IP}(i\omega) = Z_R(i\omega) + Z_C(i\omega)$$

Parallel
connection:

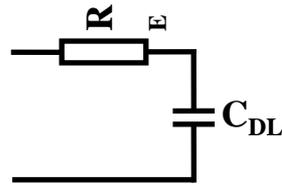


$$1/Z(i\omega) = 1/Z_R(i\omega) + 1/Z_C(i\omega)$$

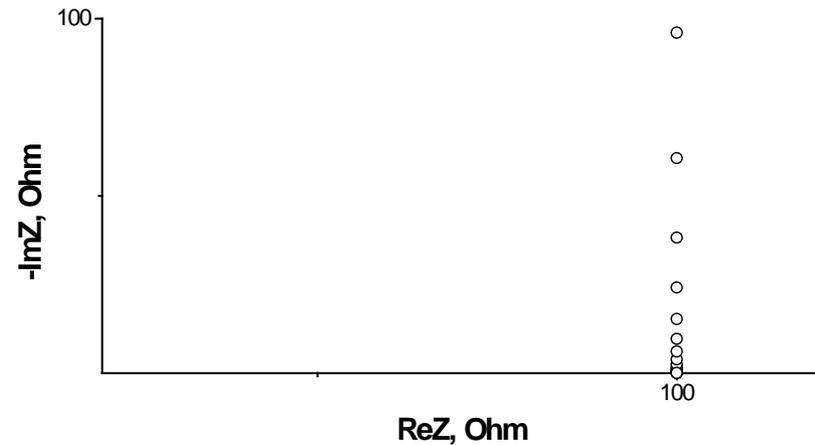


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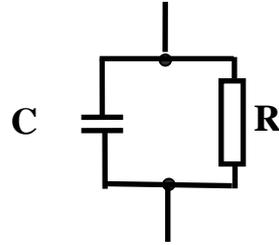
$$\begin{aligned} Z(i\omega) &= Z_R(i\omega) + Z_C(i\omega) = \\ &= R + (i\omega C)^{-1} = R - i(\omega C)^{-1} \end{aligned}$$





➤ Connections between elements:

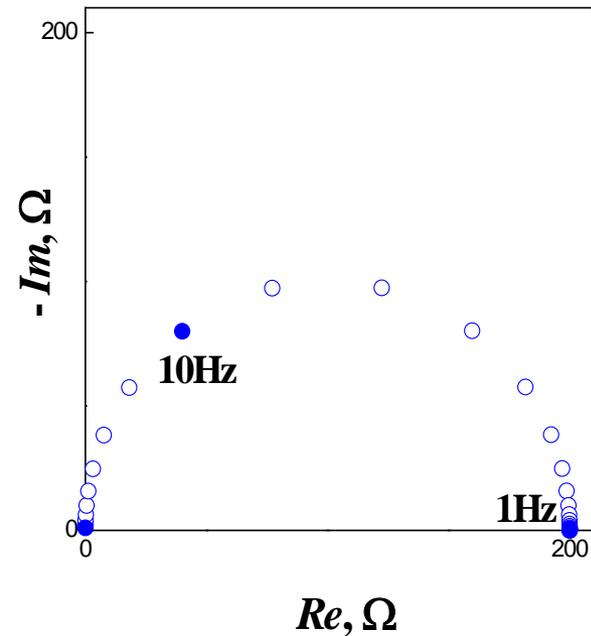
Parallel connection:



$$1/Z(i\omega) = 1/Z_R(i\omega) + 1/Z_C(i\omega)$$

$$\frac{1}{Z(i\omega)} = \frac{1}{Z_R(i\omega)} + \frac{1}{Z_C(i\omega)}$$

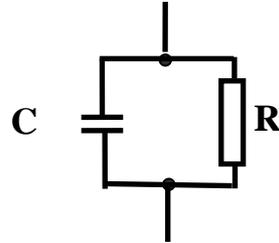
$$T = R \cdot C$$





➤ Connections between elements:

Parallel connection:

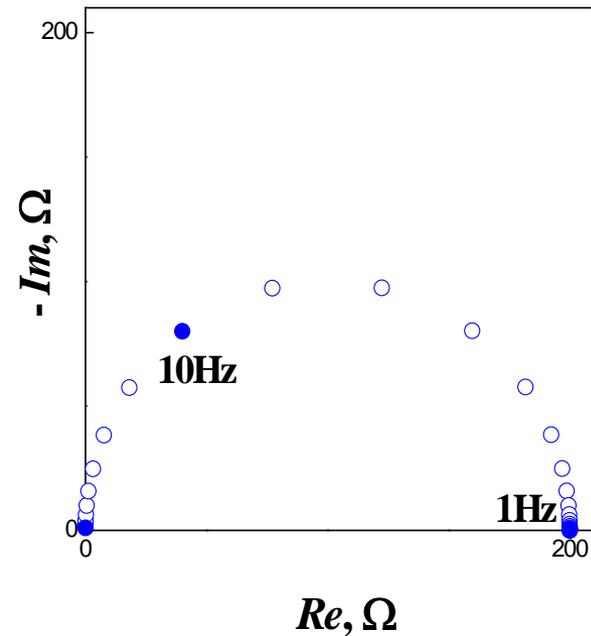


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$$\frac{1}{Z(i\omega)} = \frac{1}{Z_R(i\omega)} + \frac{1}{Z_C(i\omega)}$$

$$Z(i\omega) = \frac{R}{1 + \omega^2 T^2} + i \frac{\omega R T}{1 + \omega^2 T^2}$$

$$T = R \cdot C$$



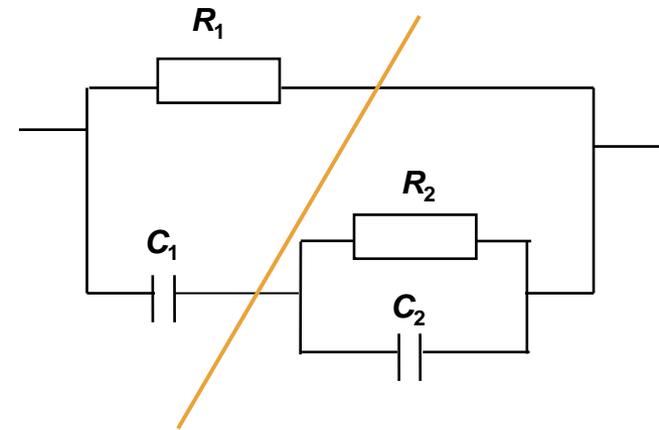


- ✓ Ladder Structure – consists of a number of kernels corresponding to the modelled phenomena. The modeled phenomena occur consequently.

$$Z(i\omega) = Z_1(i\omega) + \{Z_2(i\omega) + [Z_3(i\omega) + Z_4(i\omega) + \dots]^{-1}\}^{-1}$$

The model has typical “ladder” structure

Application for description of processes at the electrode interface





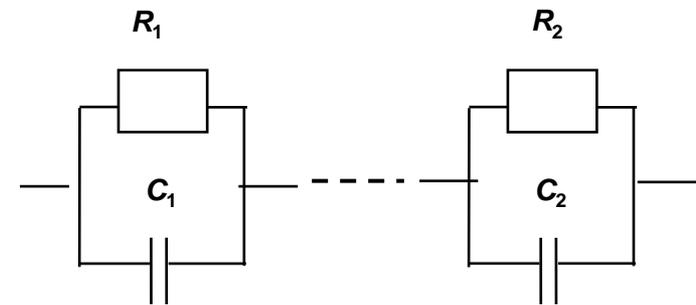
- ✓ Voigt's Structure – consists of meshes with impedances $Z_k(i\omega)$, connected in series.

$$Z(i\omega) = \sum Z_k(i\omega)$$

The phenomena modeled by each mesh start instantaneously.

The flowing current is equal for all meshes.

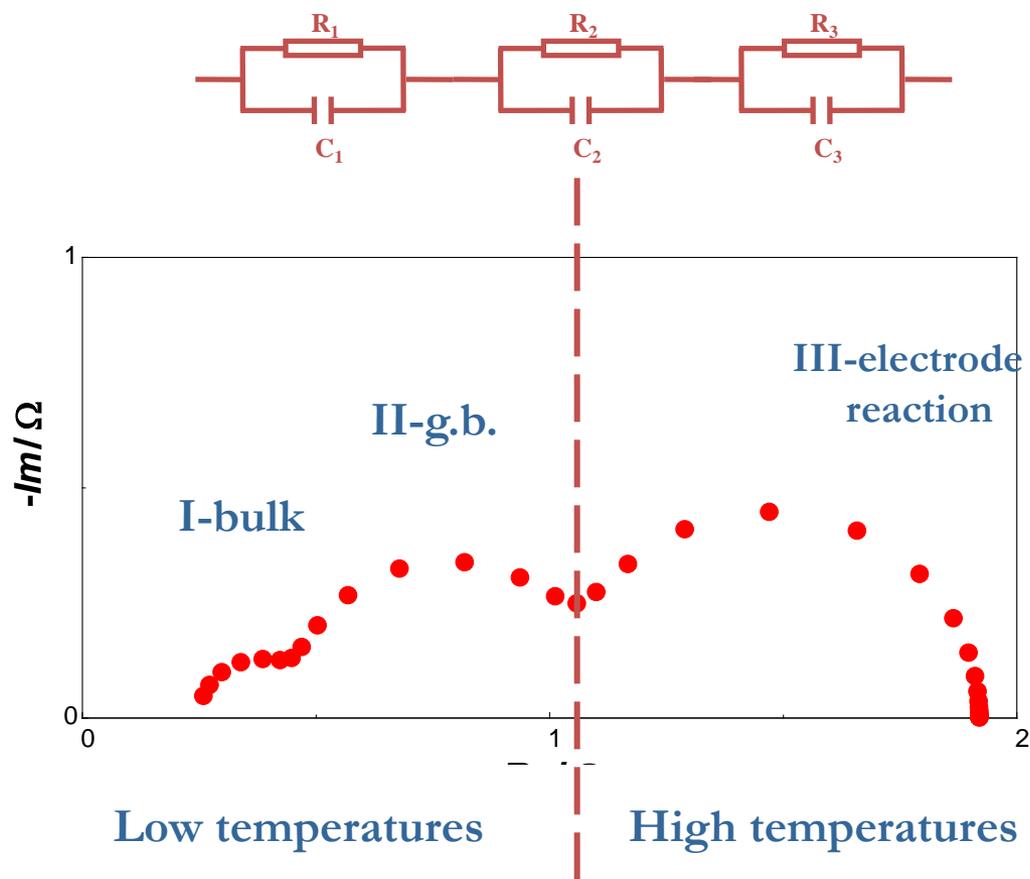
The rates depend on their own time-constants.



Voigt's model structure is applied for impedance description of solid state samples



➤ Main model structures: Voigt's model structure





➤ Model description conventions

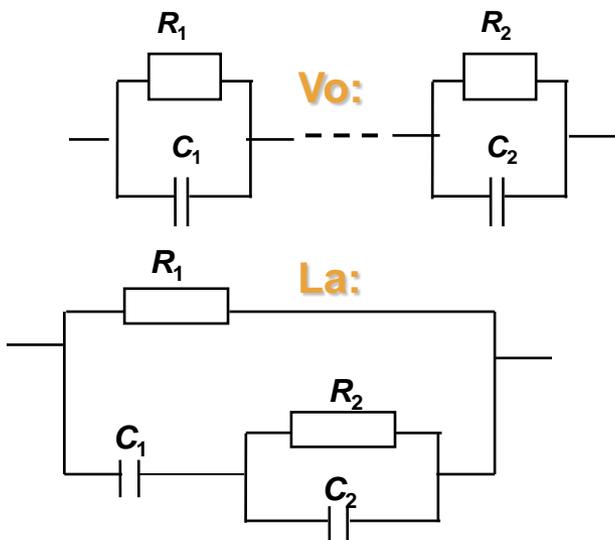
✓ Structures:

La: - ladder; Vo: - Voigt

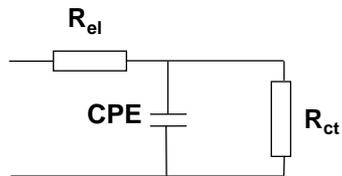
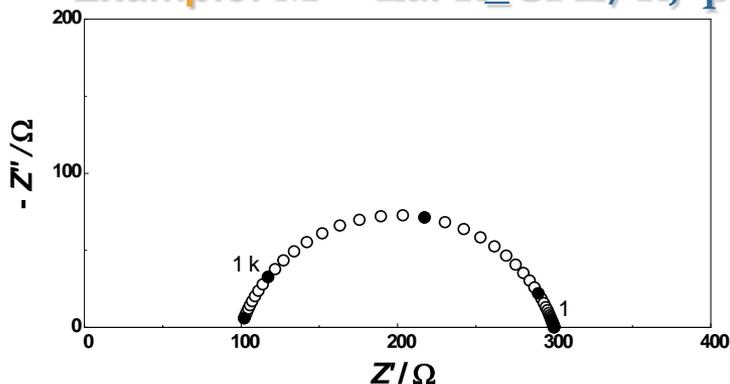
✓ Elements: R, C, L, W, BW, CPE, BCP

✓ Connections: “ ” in series; “/” in parallel

✓ Parameters: dimensions in SI ; delimiters “;”; multiple parameters separator – “\”



Example: $M = \text{La: } R_CPE/R;$ par: 100; $10^{-3} \setminus 0.8;$ 200



IUPAC project: Z. Stoykov (coordinator)
Ch. Brett, M. Orazem



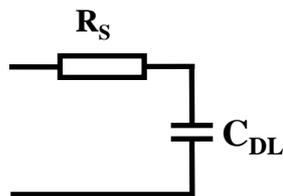


- ✓ Ideally polarizable electrode (IPE) $La: R_s C_{dl}$

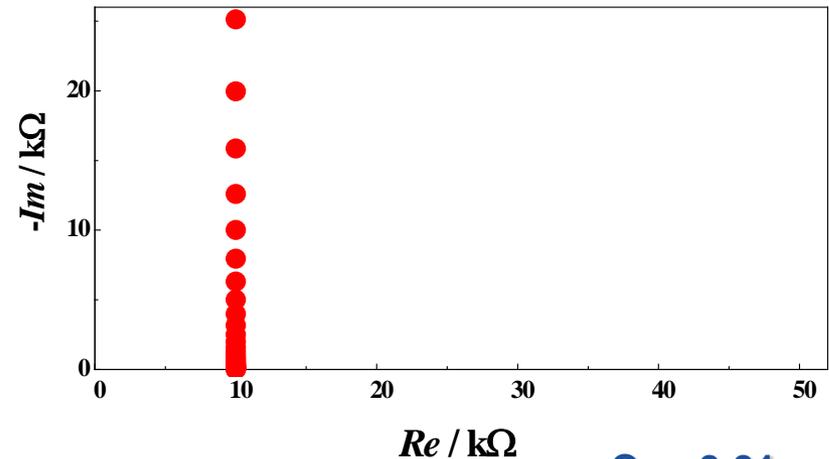
describes a case when there is
absence of any process at the
electrode surface

Structure (equivalent circuit)

Impedance



$$Z_{IPE}(i\omega) = R_s - i(\omega C_{dl})^{-1}$$



$C_{DL}=0.01$
 $R_s=10E+3$
 $R_s=20E+3$
 $R_s=30E+3$

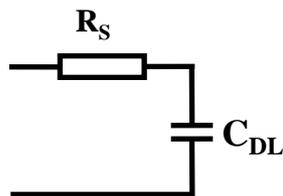


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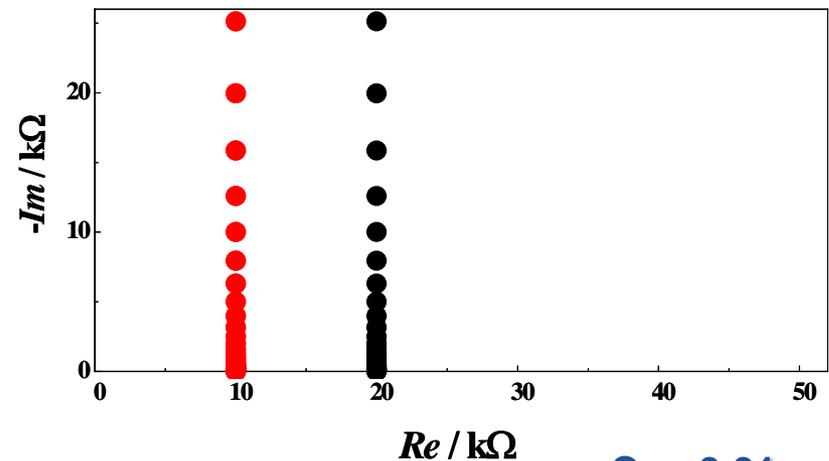
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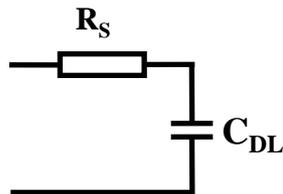


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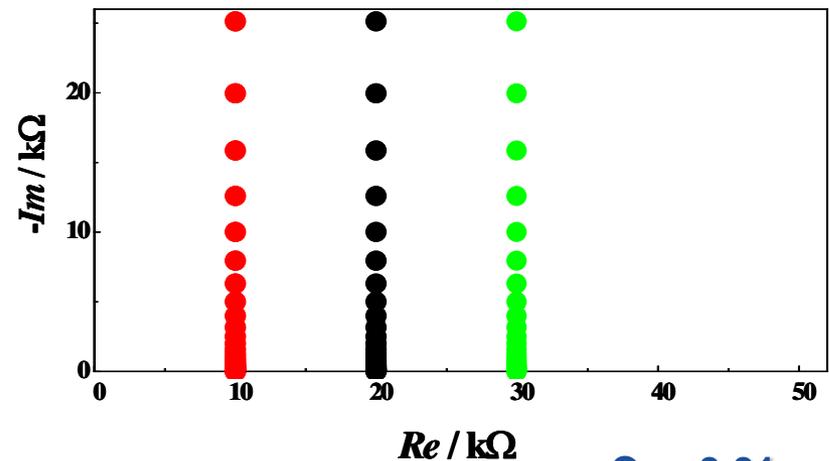
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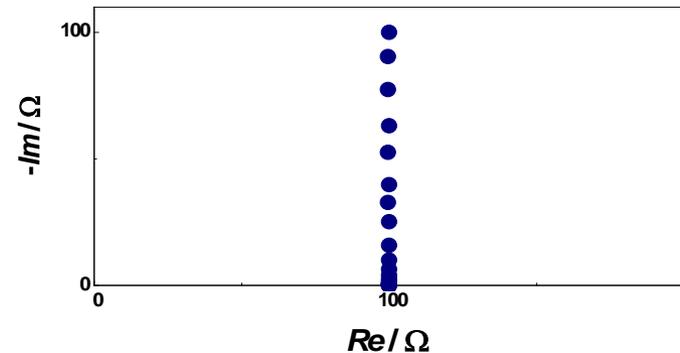
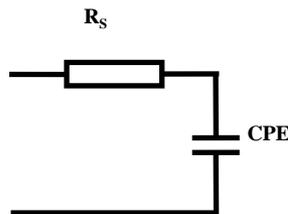
✓ Modified Ideally polarizable electrode (MIPE) La: R_s CPE_{dl}

describes a case when the electrode surface is rough and inhomogeneous

$R_s = 100$
 $A = 0.01$
 $n = 1$
 $n = 0.8$

Structure (equivalent circuit)

Impedance



$$Z_{\text{MIPE}}(i\omega) = R_s + A^{-1} (i\omega)^{-n}$$

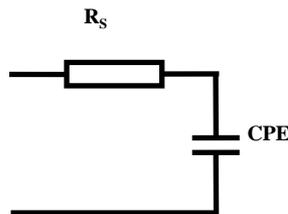


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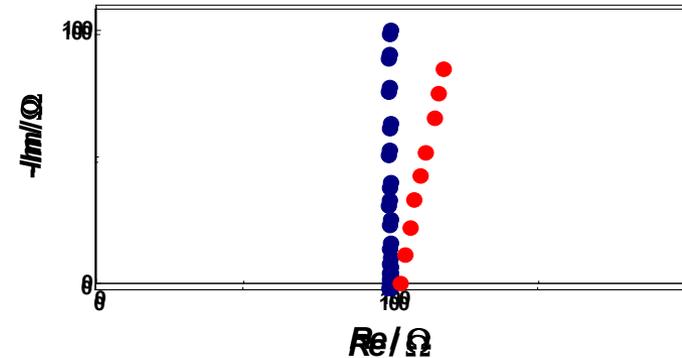
Structure (equivalent circuit)

Impedance



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$R_s = 100$
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 $n = 1$
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- ✓ Polarizable electrode (PE) (simple Faradaic reaction) **La:** R_s C_{dl}/R_{ct}

Describes a single step
electrochemical reaction at the
electrode surface

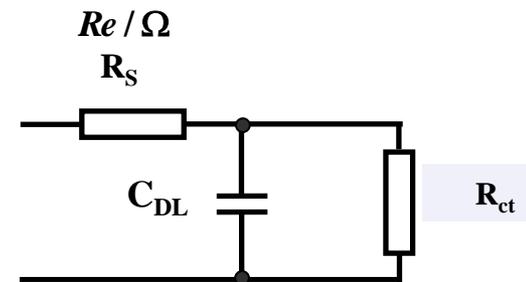
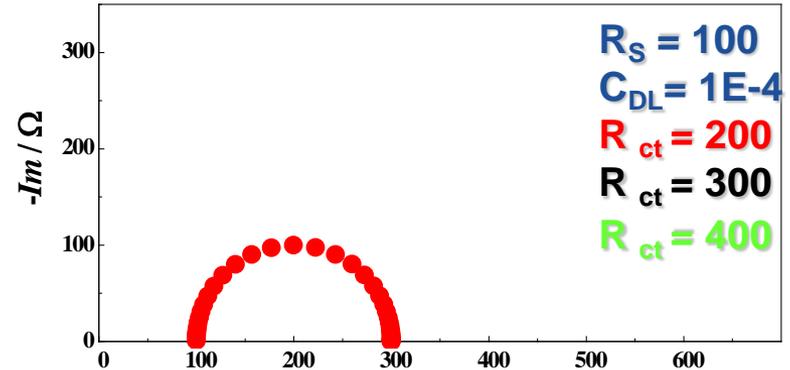
Additiveness of the Faradaic
current and the charging
current of the double layer

Structure (equivalent circuit)-
physical meaning

Impedance

$$Z_{PE}(i\omega) = R_s + R_{ct}(1 + \omega^2 T^2)^{-1} - i\omega R_{ct} T (1 + \omega^2 T^2)^{-1}$$

$$(T = RC)$$





- ✓ Polarizable electrode (PE) (simple Faradaic reaction) **La:** R_s C_{dl}/R_{ct}

Describes a single step
electrochemical reaction at the
electrode surface

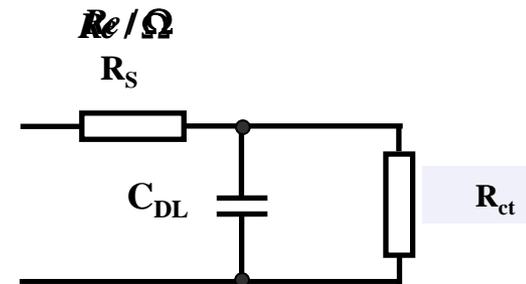
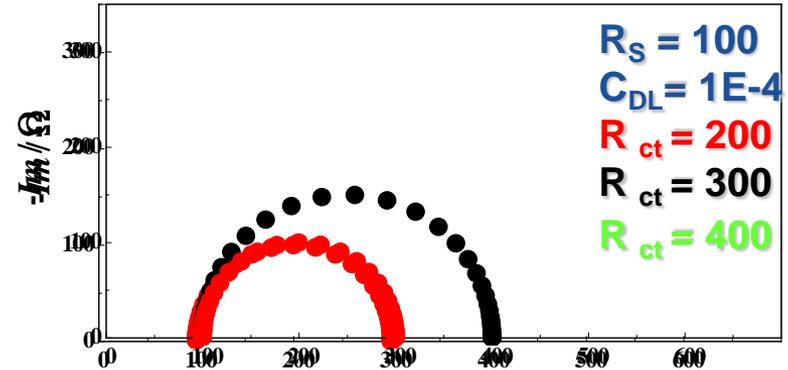
Additiveness of the Faradaic
current and the charging
current of the double layer

Structure (equivalent circuit)-
physical meaning

Impedance

$$Z_{PE}(i\omega) = R_s + R_{ct}(1 + \omega^2 T^2)^{-1} - i\omega R_{ct} T (1 + \omega^2 T^2)^{-1}$$

$$(T = RC)$$





- ✓ Polarizable electrode (PE) (simple Faradaic reaction) **La:** R_s C_{dl}/R_{ct}

Describes a single step
electrochemical reaction at the
electrode surface

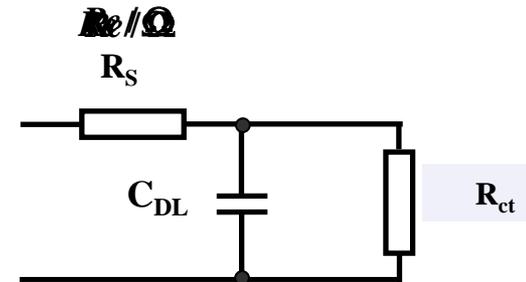
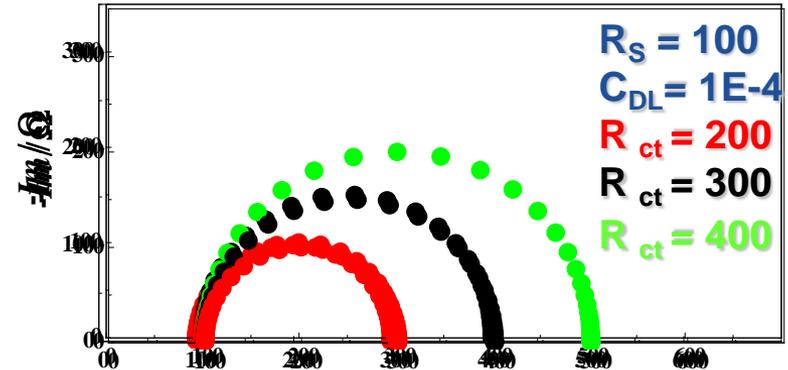
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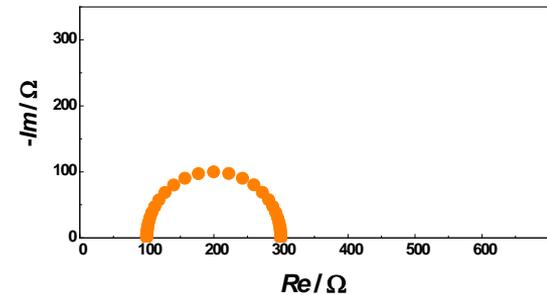
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$$(T = RC)$$

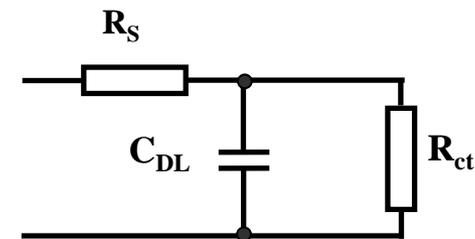




Geometrically the impedance diagram is presented as an **ideal semicircle** with a **diameter R_{ct}** ;
for $\omega \rightarrow \infty$ the semi-circle intercepts the real axis in R_s
for $\omega \rightarrow 0$ the intercept is in a point with value $R_s + R_{ct}$
the imaginary component reaches a **maximum** at the so called **characteristic frequency ω_0**



Impedance diagram in the frequency range 10^5 -10 Hz



$$\begin{aligned} R_s &= 100 \\ C_{DL} &= 1E-4 \\ R_{ct} &= 200 \end{aligned}$$

$$\omega_0 = (C_{dl}R_{ct})^{-1} = T^{-1} \quad (T \text{ is the time-constant})$$

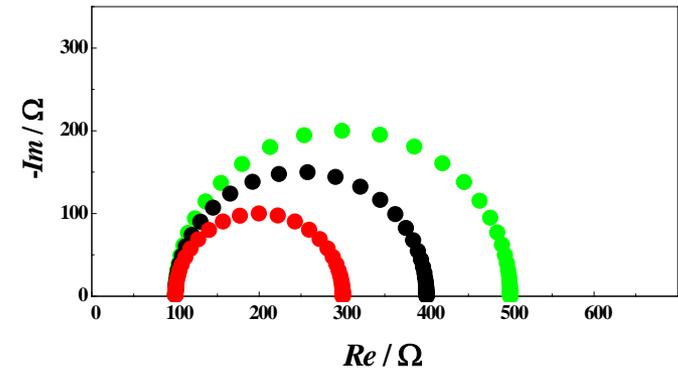


$$Z_{PE}(i\omega) = R_s + R_{ct}(1 + \omega^2 T^2)^{-1} - i\omega R_{ct} T (1 + \omega^2 T^2)^{-1}$$

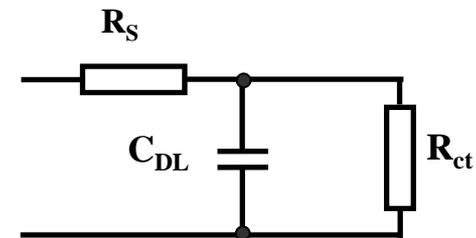
The structural parameters have direct physical meaning (R_s, R_{ct}, C_{dl}) for partially reversible charge transfer reaction at equilibrium

$$R_{ct} = (RT/nF)(1/I_0) \quad (I_0 - \text{exchange current})$$

R_{ct} depends on the rate of reaction, which is potential dependent and thus R_{ct} varies with the potential, i.e. the diameter of the semi-circle changes.



Impedance diagram in the frequency range 10^5 -10 Hz

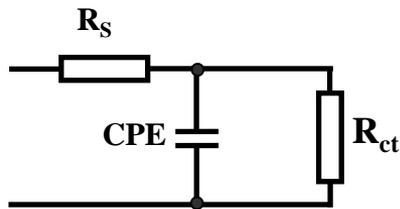


$R_s = 100$
 $C_{DL} = 1E-4$
 $R_{ct} = 200$
 $R_{ct} = 300$
 $R_{ct} = 400$
 $R_{ct} = 500$





- ✓ Modified Polarizable electrode (MPE) La: R_s CPE_{dl}/R_{ct}



$$R_{EIS} = 100$$

$$R_{ct} = 200$$

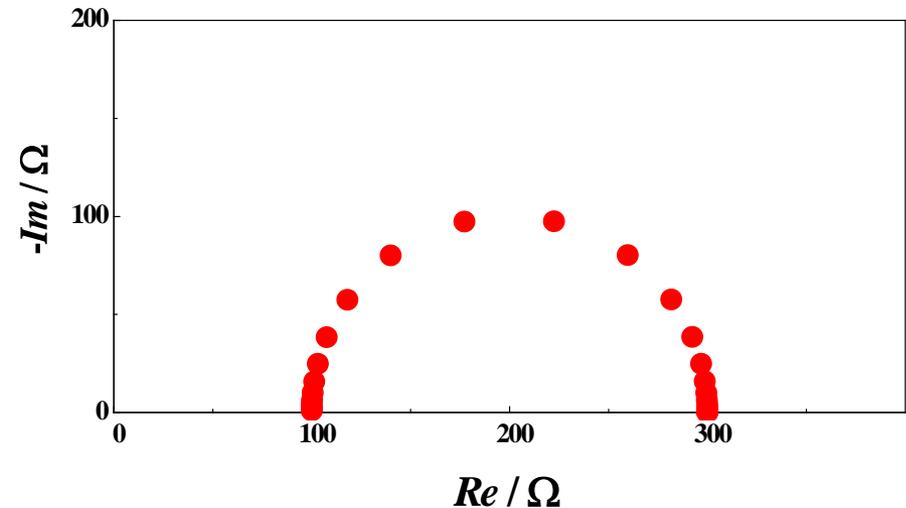
$$A = 0.01$$

$$n = 1$$

$$n = 0.8$$

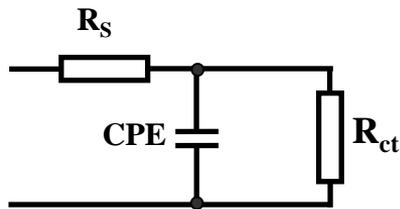
May give better Structure, but formal description of the investigated system

May have a physical meaning: description of the electrode's surface roughness





- ✓ Modified Polarizable electrode (MPE) La: R_s CPE_{dl}/R_{ct}



$$R_{EIS} = 100$$

$$R_{ct} = 200$$

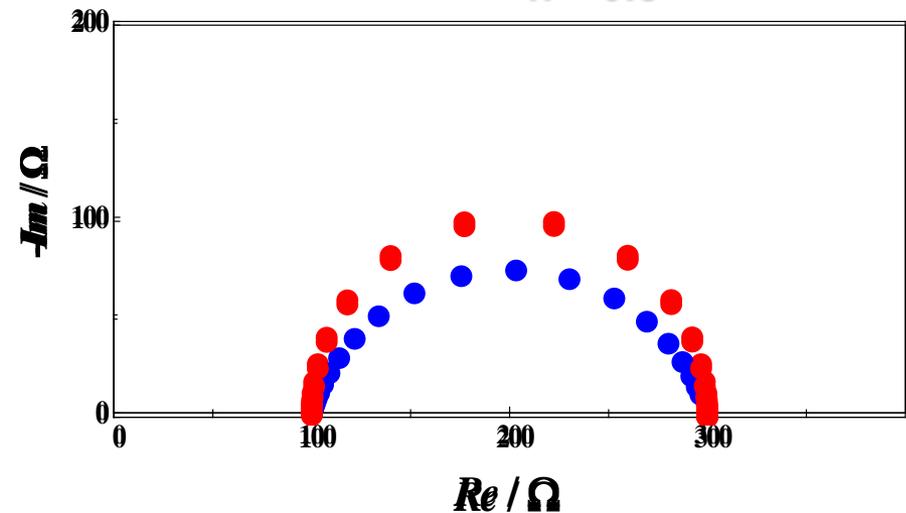
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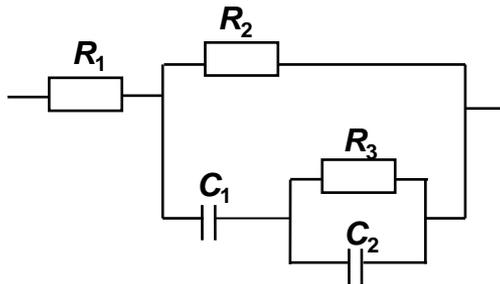
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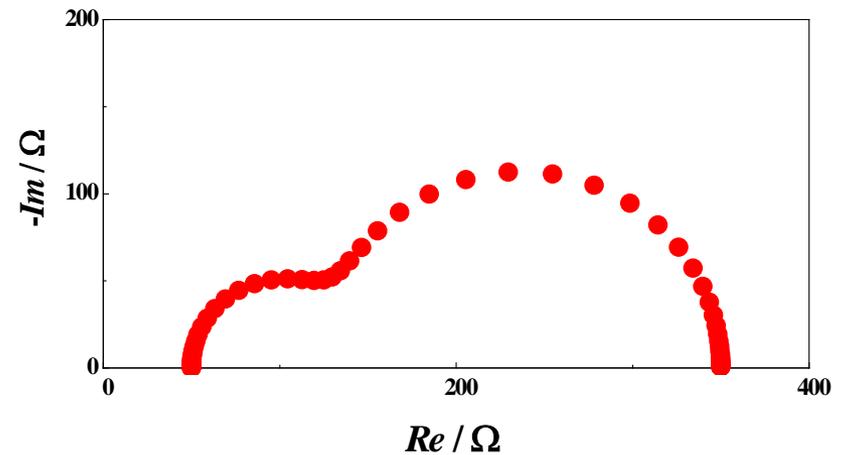


- ✓ Faradaic reaction with one adsorbed species **La: $R_1 C_1/R_2 C_2/R_3$**

Structure (equivalent circuit)



describes a heterogeneous
reaction occurring in two steps
with adsorption of the
intermediate product X

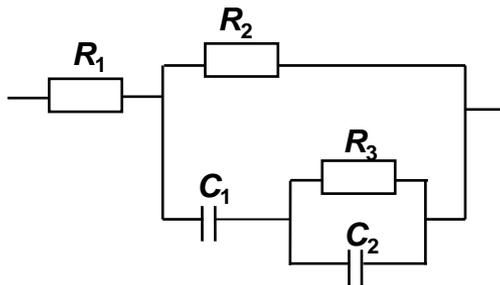


$$\begin{aligned} R_1 &= 50 \\ R_2 &= 100 \\ C_1 &= 1E-3 \\ R_3 &= 200 \\ C_2 &= 1E-2 \\ C_2 &= 3E-3 \\ C_2 &= 1E-3 \end{aligned}$$

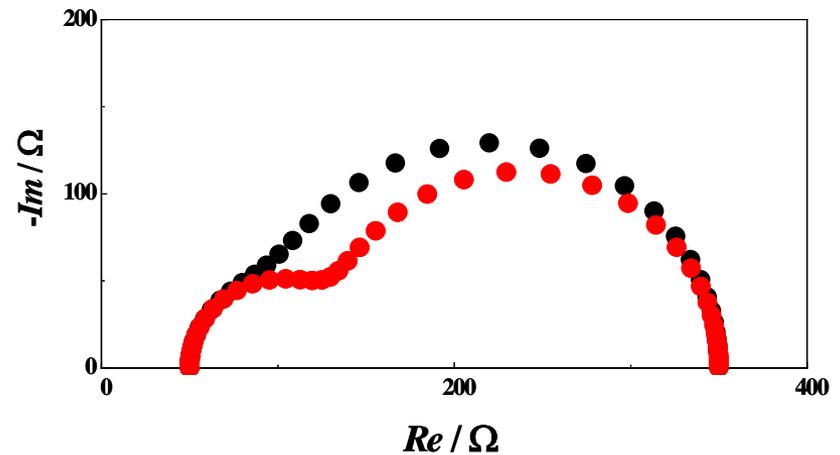


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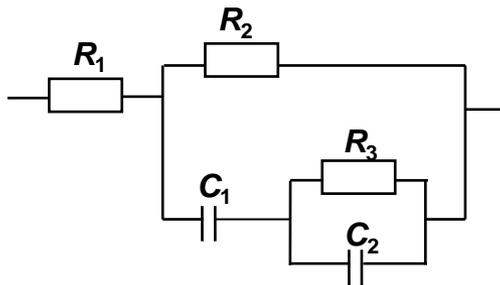


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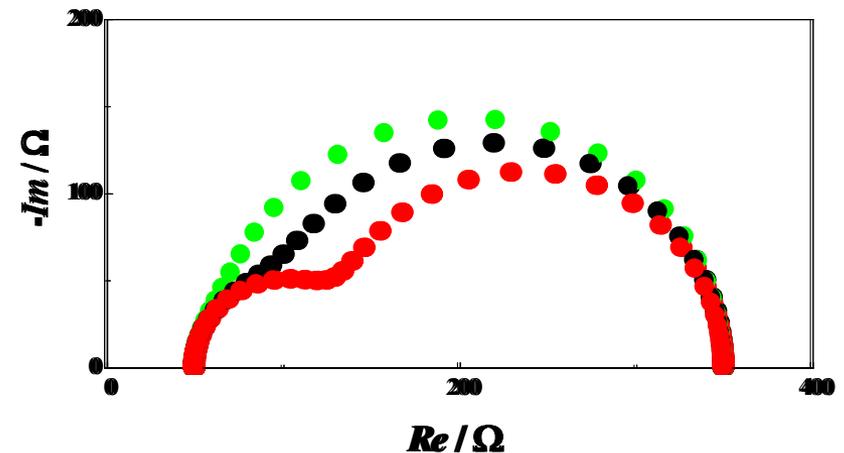


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Structure (equivalent circuit)



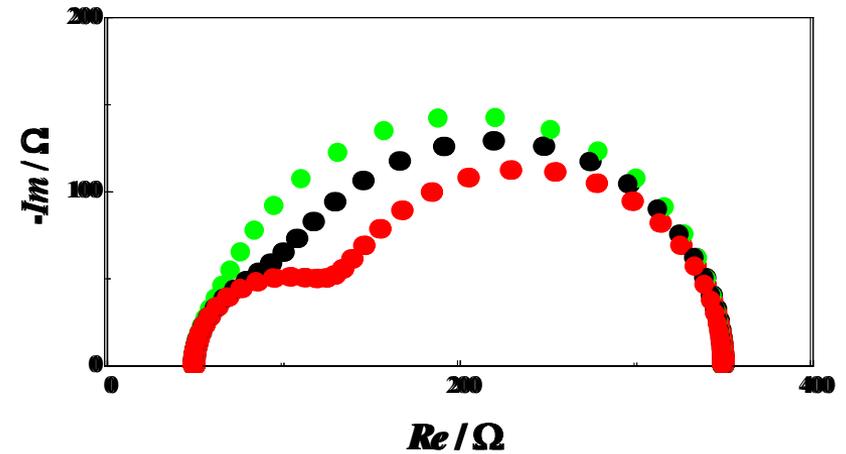
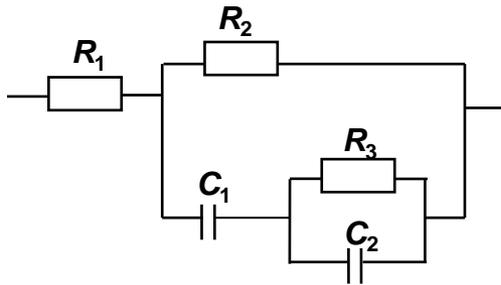
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- ✓ Faradaic reaction with one adsorbed species $La: R_1 C_1/R_2 C_2/R_3$



The structural parameters have direct physical meaning:

$$R_1 = R_s \quad C_1 = C_{DL}$$

$$R_2 = R_{ct} \quad C_2 = C_{ad}$$

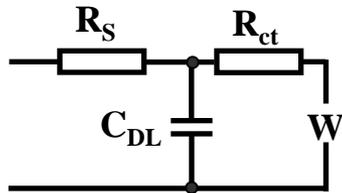
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✓ Randles model $La: R_s C_{dl}/R_{ct} W$

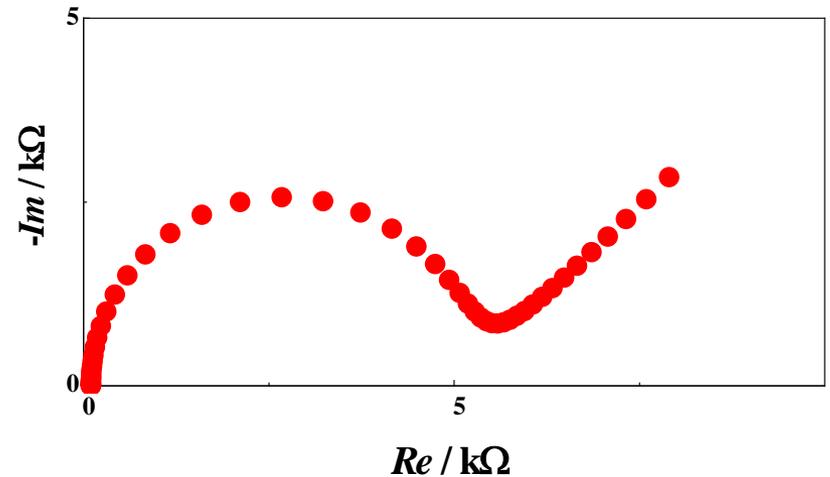
Describes polarizable electrode
with diffusion limitations

Structure (equivalent circuit)



Impedance

$$Z_{RNS}(i\omega) = R_s + [i\omega C_{dl} + (R_{ct} + \sigma\omega^{-1/2} - i\sigma\omega^{-1/2})^{-1}]^{-1}$$



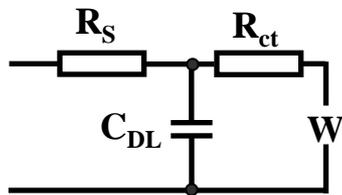
$R_s = 100$
 $R_{ct} = 5E+3$
 $W = 100$
 $C_{DL} = 3E-4$
 $C_{DL} = 1E-3$
 $C_{DL} = 3E-3$



✓ Randles model $La: R_s C_{dl}/R_{ct} W$

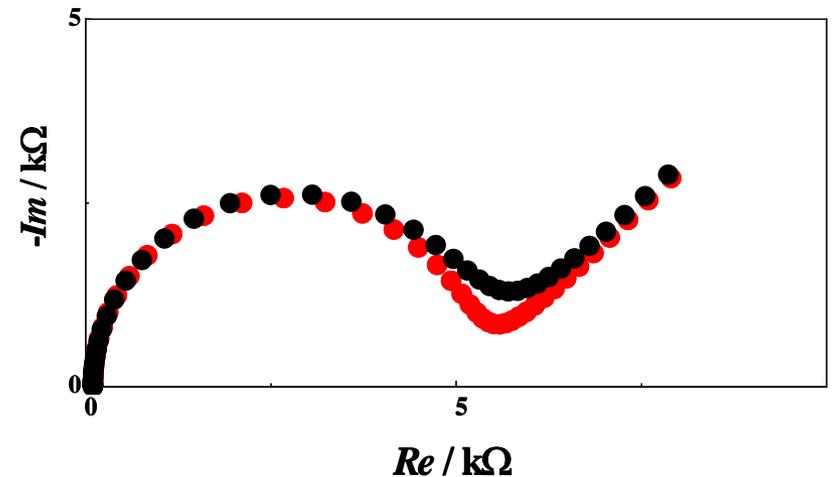
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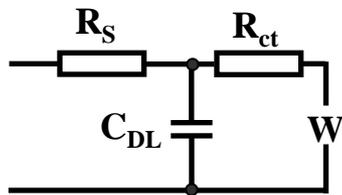
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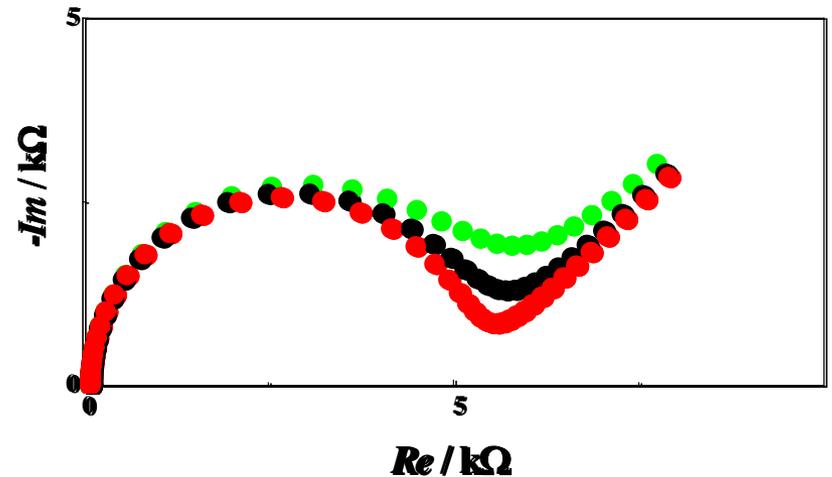
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 $W=100$
 $C_{DL}=3E-4$
 $C_{DL}=1E-3$
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Relation between the structural parameter σ and the electrochemical parameters:

$$W = R_{ct} [k_f (D_O)^{-1/2} + k_b (D_R)^{-1/2}]$$

(k_f , k_b – reaction rates of the “forward” and “backward” reactions; D_O and D_R – diffusion coefficients of the species)

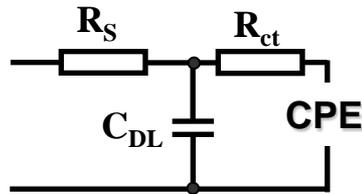
The **structural model has 4 parameters**, which can be determined from the impedance (R_S , R_{ct} , C_{dl} , W), while the **electrochemical impedance model has 7 parameters** (R_S , C_{dl} , I_0 , k_f , k_b , D_R , D_O), which can not be determined directly)



✓ Modified Randles model

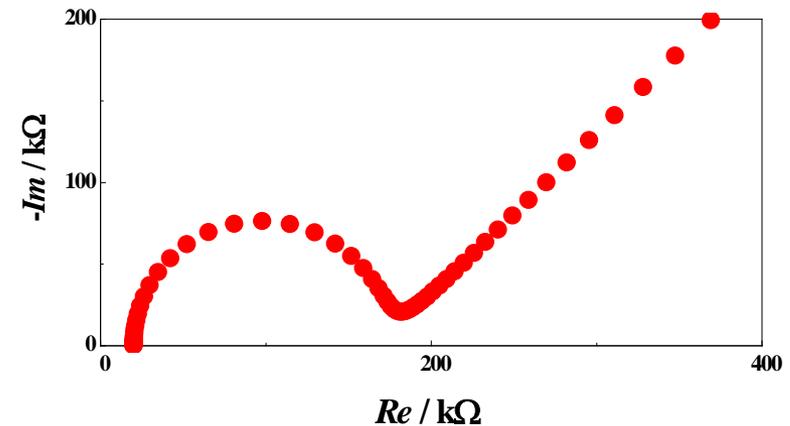
La: $R_s C_{dl}/R_{ct}$ CPE

Structure (equivalent circuit)



Describes geometrical or activation inhomogeneity of the surface or deviations from the linear diffusion process.

That happens very often when the diffusion occurs in a diluted solution or in case that the diffusion does not obey Fick's



$$R_s = 20$$

$$R_{ct} = 150$$

$$C_{DL} = 1E-2$$

$$A = 0.1$$

$$n = 0.5$$

$$n = 0.45$$

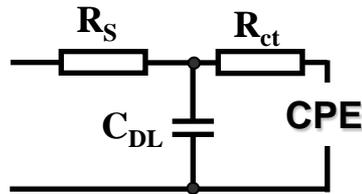
$$n = 0.4$$



✓ Modified Randles model

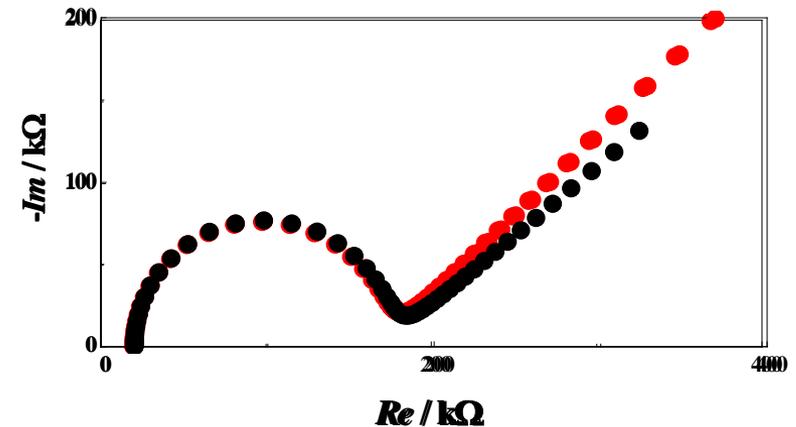
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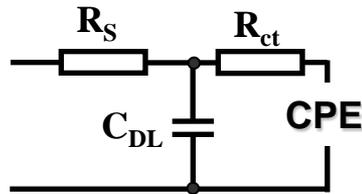
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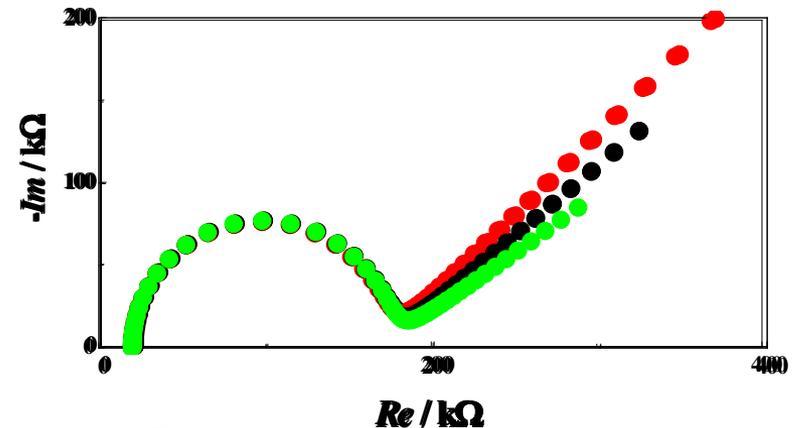
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$$n = 0.45$$

$$n = 0.4$$



- ✓ Impedance does not measure directly a physical phenomenon
- ✓ Interpretation of experimental data - construction of an impedance model by identification procedure.

Parametric identification approach – confirmation of preliminary chosen hypothetical model(s)

Structural identification approach derives structure + parameters from experimental data



1. Why Impedance

2. What is impedance

3. Impedance measurements

- Basic Working Hypotheses

4. Presentation of the experimental data

5. Interpretation of the measured data (data analysis)

- Impedance elements
- Simple models
- Identification

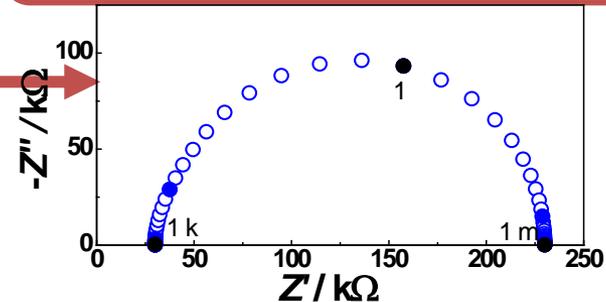


STEP I

Organization of the experiment & measurement
Monitoring, data pre-processing

➤ Algorithm of one impedance experiment

$D_3 [Re_i, Im_i, \omega_i]$



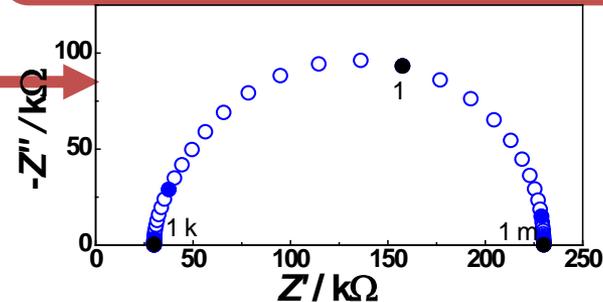


➤ Algorithm of one impedance experiment

STEP I

Organization of the experiment & measurement
Monitoring, data pre-processing

$D_3 [Re_i, Im_i, \omega_i]$



STEP II

DATA ANALYSIS

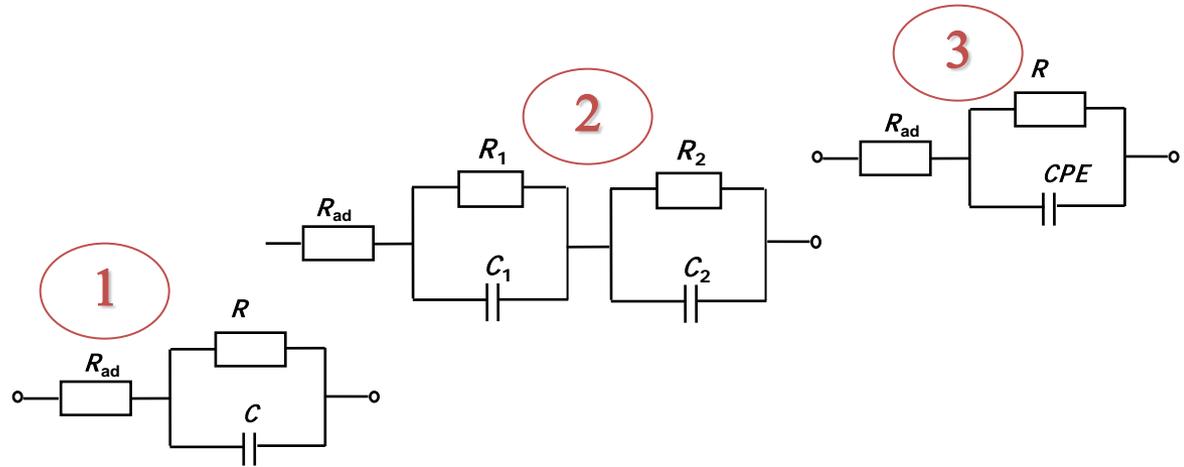
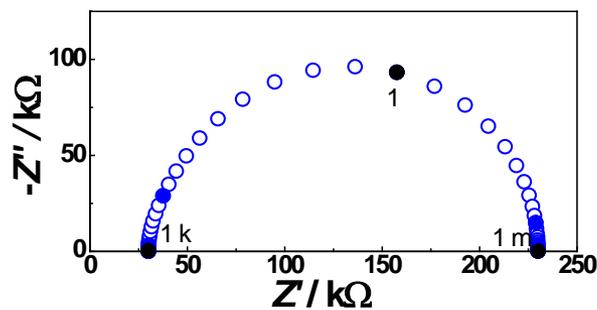
Model Identification

Parametric Identification Approach



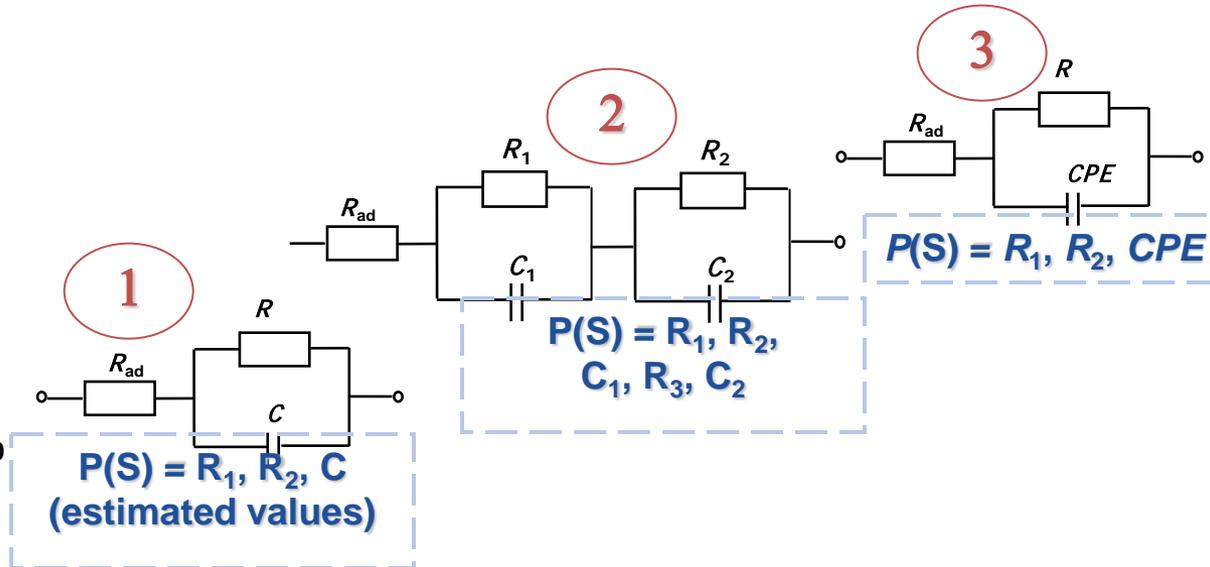
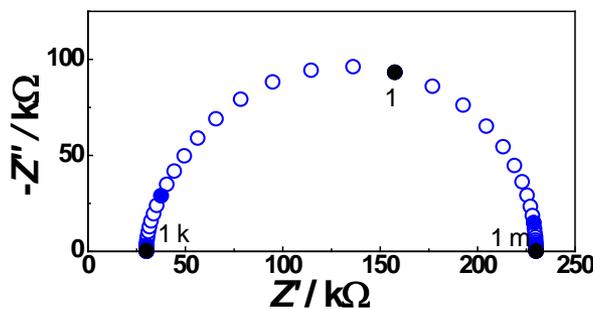


➤ Choice of a working hypothesis presented by one or few models





➤ Choice of a working hypothesis presented by one or few models



➤ Parametric identification $\hat{P}_M = \text{Par. Ident.}[\omega_i, \text{Re}_i, \text{Im}_i | S_M]$

➤ Model validation



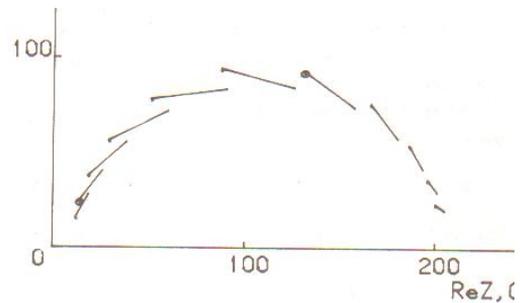


➤ Model validation

✓ Model simulation: $\hat{Z}(i\omega) = \text{Simul.}[\omega_i, |S_M, \hat{P}_M]$

✓ Selection of criterion for proximity $\Delta_i(i\omega) = \Phi_i(\hat{Z}_i - Z_i)$

✓ Analysis of the residuals (adequacy) $\Delta_i(i\omega) = f(\lg f)$



➤ Selection of the best model



➤ Selection of the Best Model

Evaluation of the distance for “best fit “

$$\sum \Delta^2_i \Rightarrow \min$$

The most frequently applied algorithm for parametric identification

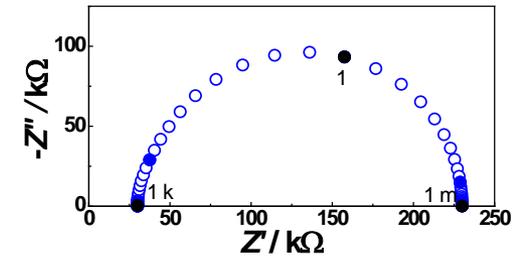
Complex Nonlinear Least Squares Method (CNLS).

Professional software tools are available for it !!!



D3 [Re_i , Im_i , ω_i]

I. Measurement & Data Pre-Processing
II. Data Analysis

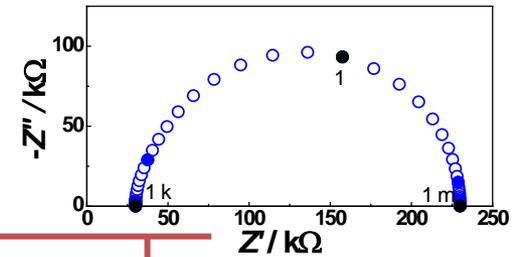




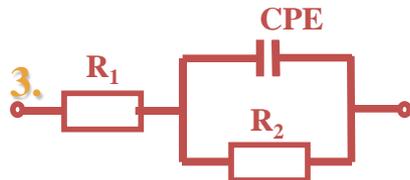
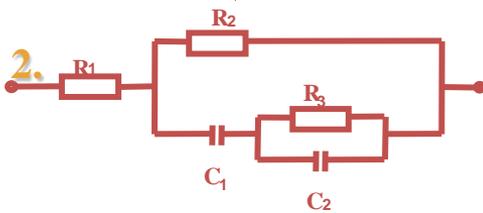
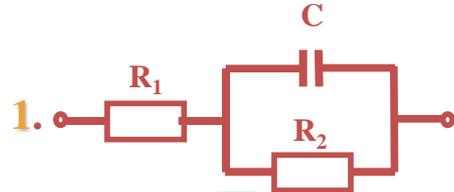
D3 [Re_i , Im_i , ω_i]

I. Measurement & Data Pre-Processing

II. Data Analysis



1. Choice of Hypothetical model(s)

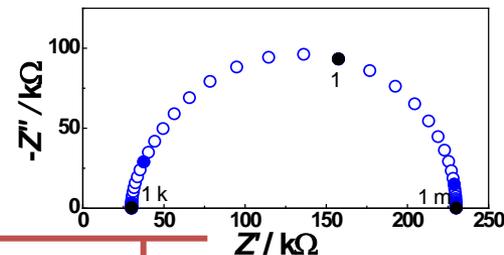




D3 [Re_i, Im_i, ω_i]

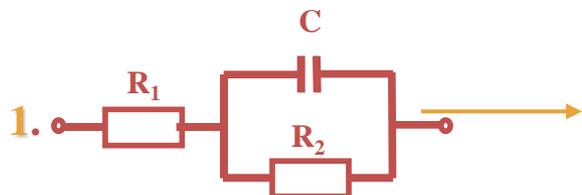
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II. Data Analysis



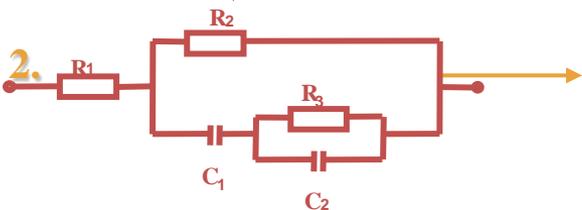
1. Choice of Hypothetical model(s)

2. Parametric Identification & Validation (CNLS)

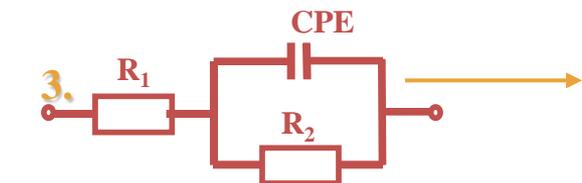


$$P(s) = R_1, R_2, C$$

(estimated values)



$$P(s) = R_1, R_2, C_1, R_3, C_2$$



$$P(s) = R_1, R_2, CPE$$

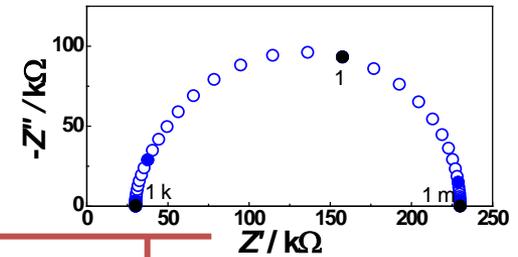
No adequacy



D3 [Re_i , Im_i , ω_i]

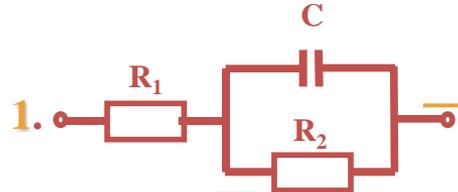
I. Measurement & Data Pre-Processing

II. Data Analysis

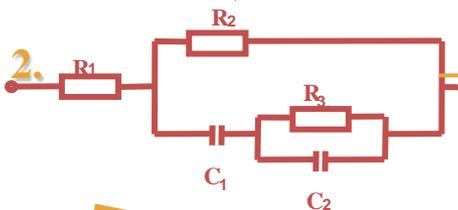


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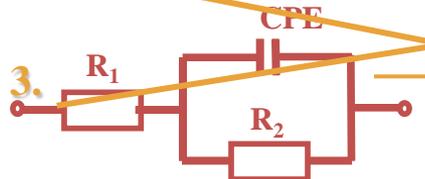
2. Parametric Identification & Validation (CNLS)



$P(s) = R_1, R_2, C$
(estimated values)



$P(s) = R_1, R_2, C_1, R_3, C_2$



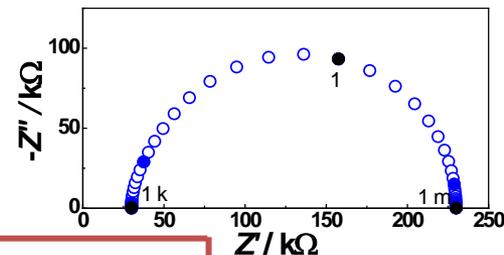
$P(s) = R_1, R_2, CPE$
No adequacy



D3 [Re_i, Im_i, ω_i]

I. Measurement & Data Pre-Processing

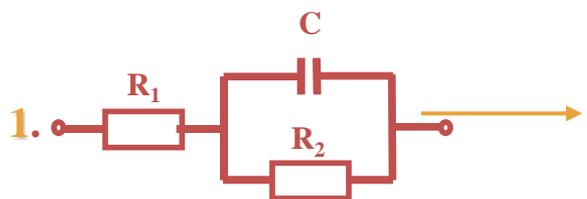
II. Data Analysis



1. Choice of Hypothetical model(s)

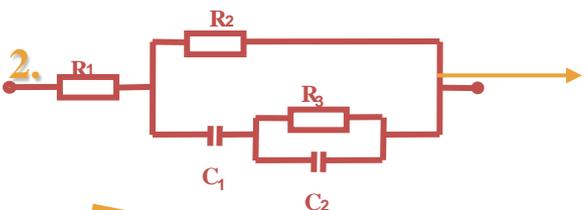
2. Parametric Identification & Validation (CNLS)

3. Selection of the **BEST** Model – “best fit”

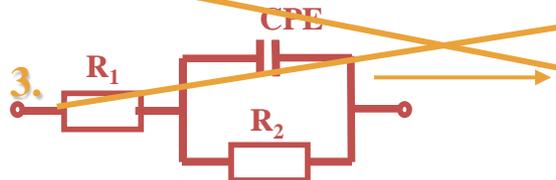


$$P(s) = R_1, R_2, C$$

(estimated values)

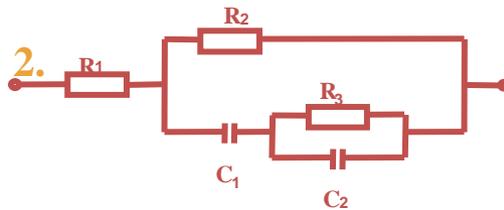
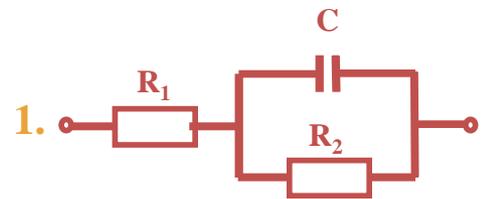


$$P(s) = R_1, R_2, C_1, R_3, C_2$$



$$P(s) = R_1, R_2, CPE$$

No adequacy

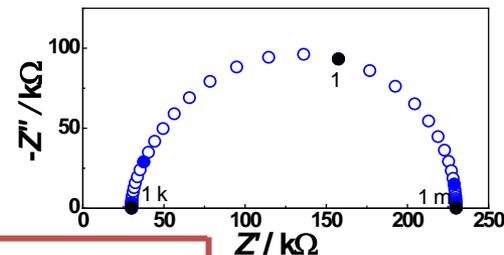




D3 [Re_i , Im_i , ω_i]

I. Measurement & Data Pre-Processing

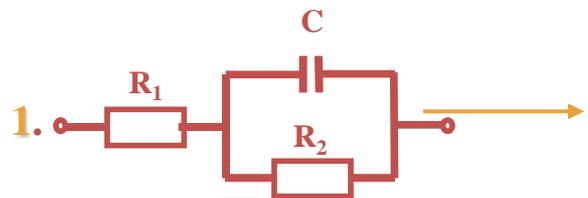
II. Data Analysis



1. Choice of Hypothetical model(s)

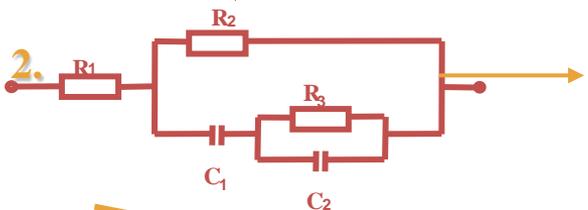
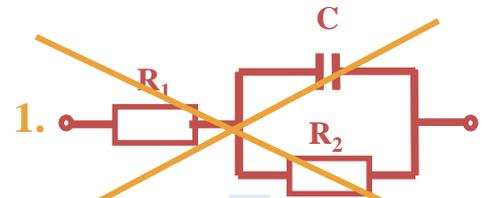
2. Parametric Identification & Validation (CNLS)

3. Selection of the **BEST** Model – “best fit”



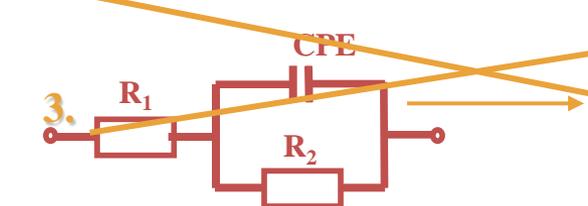
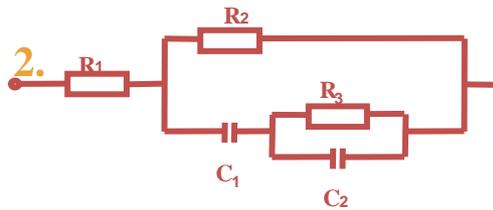
$P(s) = R_1, R_2, C$
(estimated values)

NO



$P(s) = R_1, R_2, C_1, R_3, C_2$

YES

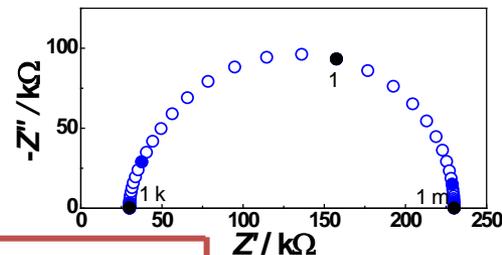


$P(s) = R_1, R_2, CPE$
No adequacy



D3 [Re_i, Im_i, ω_i]

I. Measurement & Data Pre-Processing

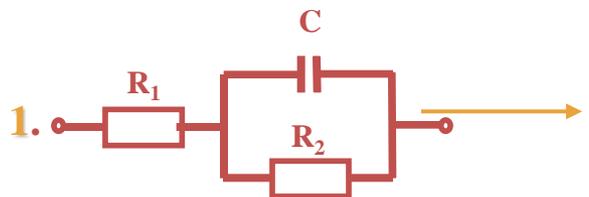


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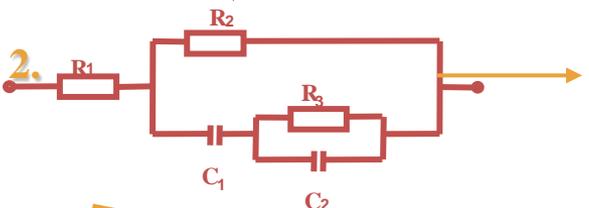
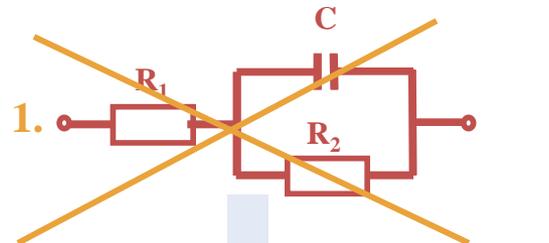
3. Selection of the **BEST** Model – “best fit”



$$P(s) = R_1, R_2, C$$

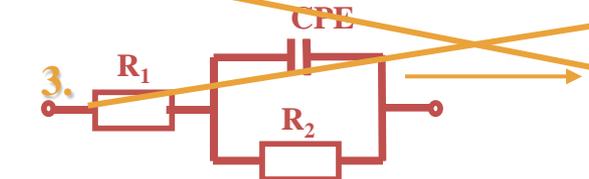
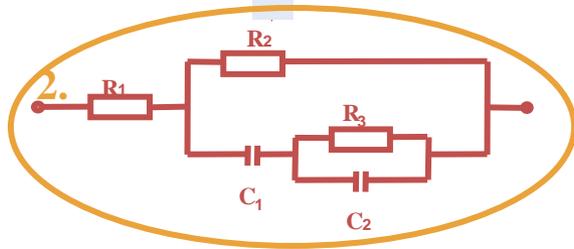
(estimated values)

NO



$$P(s) = R_1, R_2, C_1, R_3, C_2$$

YES



$$P(s) = R_1, R_2, CPE$$

No adequacy



- **GENERAL Approaches** for tailoring the materials properties
(conductivity)
 - ✓ Optimization of the composition (bulk properties)
 - ideal stoichiometric structure
 - defect structure
 - additional phases
 - composites
 - ✓ Optimization of the microstructure (grain boundary properties)
 - grain size
 - inter-granular or intra-granular pores
 - additional phases at the grain boundaries
 - architecture of ordered internal structures



➤ **GENERAL Approaches** for tailoring the materials properties
(conductivity)

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ideal stoichiometric structure
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✓ Optimization of the microstructure (grain boundary properties)

grain size
inter-granular or intra-granular pores
additional phases at the grain
boundaries
architecture of ordered internal
structures





EIS Applications in Materials Science

Voigt's model structure is applied for impedance description of solid state samples

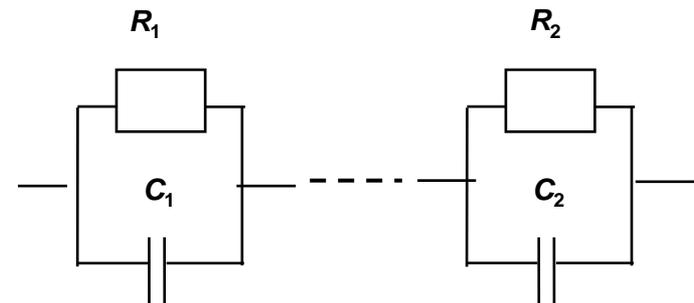
- ✓ Voigt's Structure – consists of meshes with impedances $Z_k(i\omega)$, connected in series.

$$Z(i\omega) = \sum Z_k(i\omega)$$

The phenomena modeled by each mesh start instantaneously.

The flowing current is equal for all meshes.

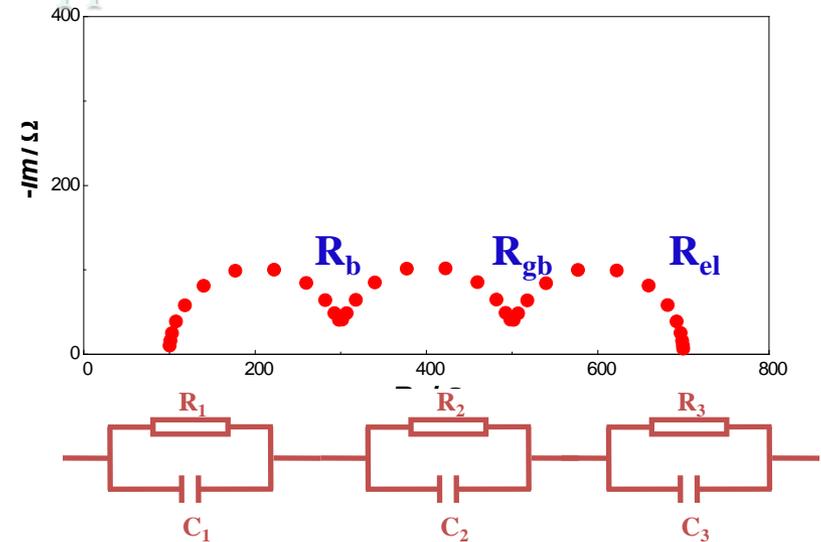
The rates depend on their own time-constants.





➤ **Basic (idealized) Model**
(~ 1970^{ths}; Bauerle & Schouler)

Voigt model structure
with 3 meshes

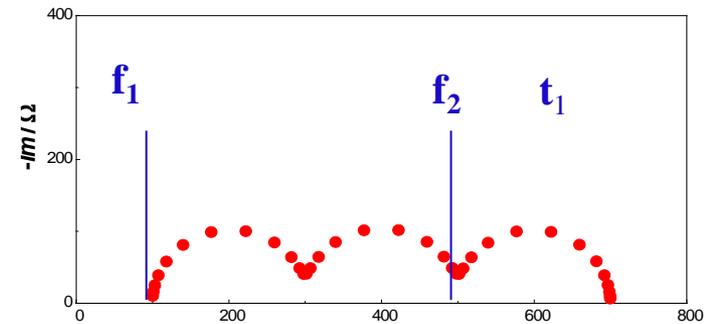


VISUALIZATION -

Depends on:

$f_1 - f_2$

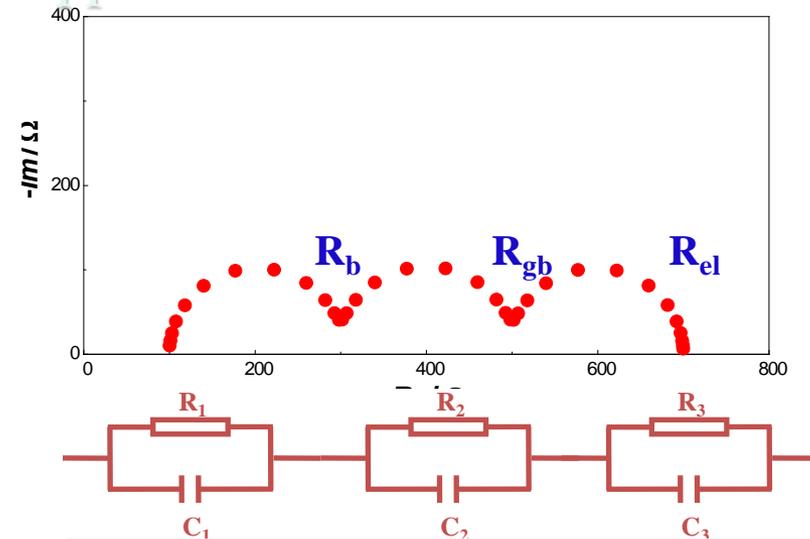
temperature





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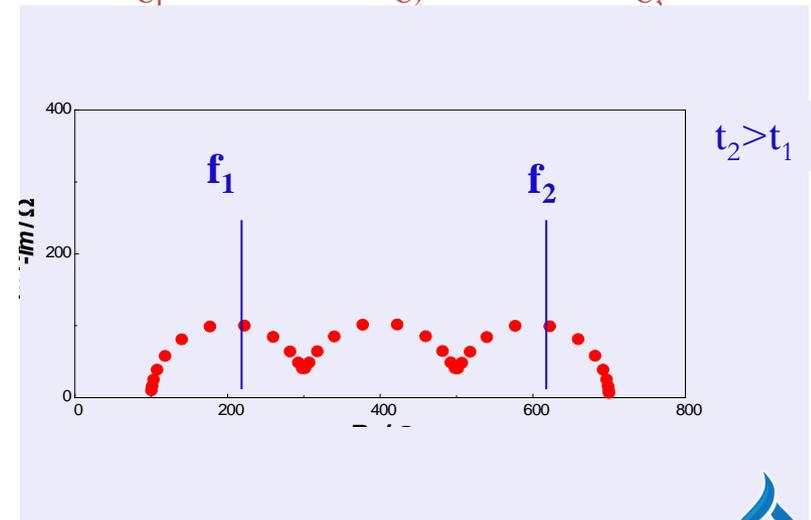


VISUALIZATION -

Depends on:

$f_1 - f_2$

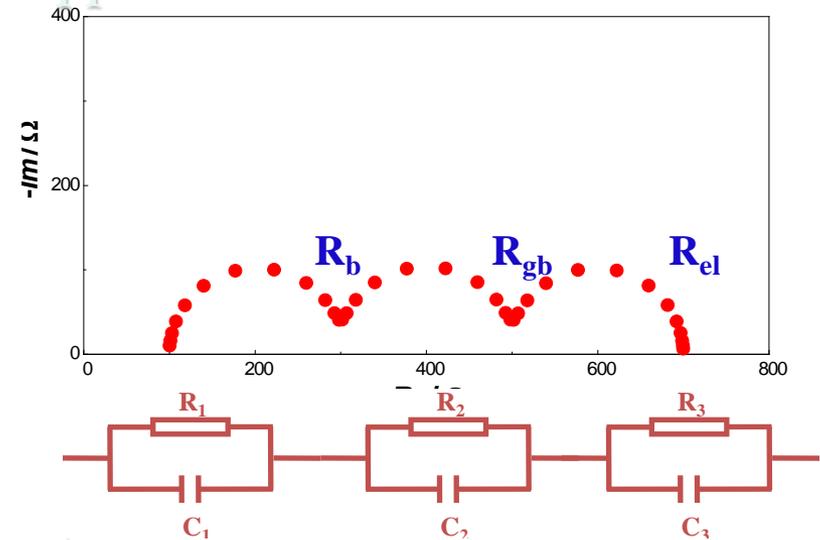
temperature





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Voigt model structure
with 3 meshes

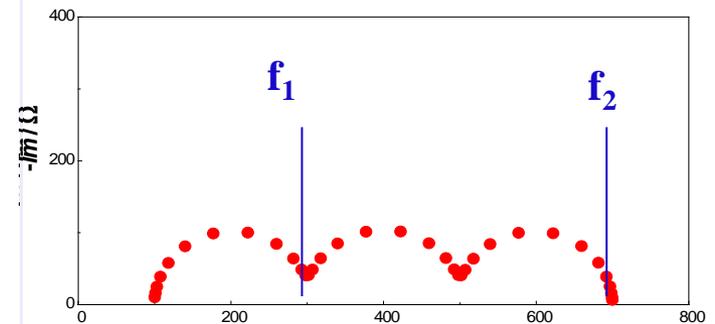


VISUALIZATION -

Depends on:

$f_1 - f_2$

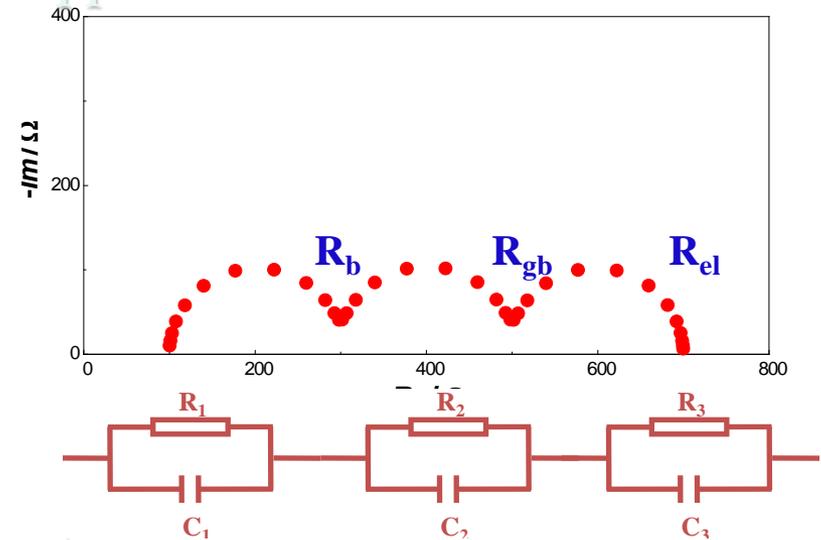
temperature





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Voigt model structure
with 3 meshes

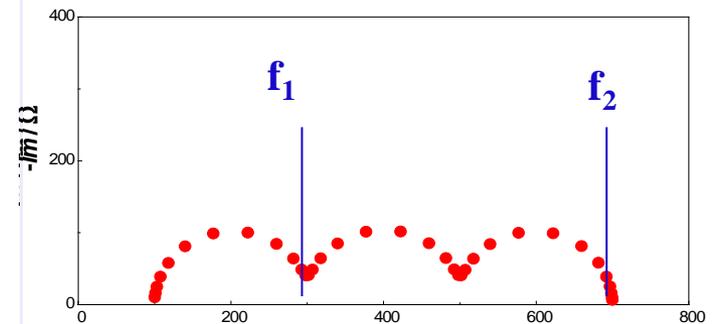


VISUALIZATION -

Depends on:

$f_1 - f_2$

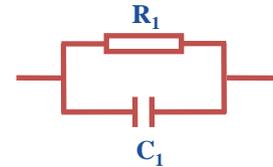
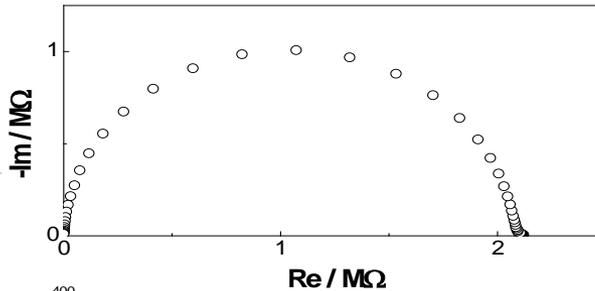
temperature





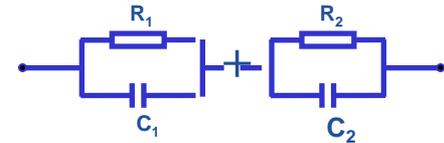
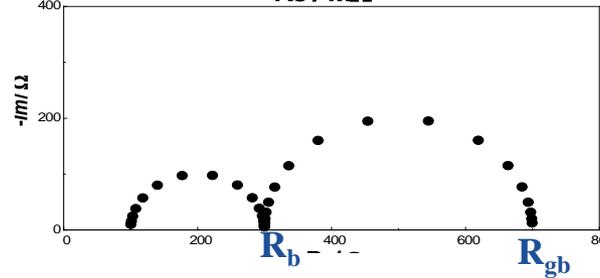
Single crystals

R_{bulk}



Polycrystalline

$R_{\text{bulk}} + R_{\text{g.b.}}$



$$R = f(T)$$

Arenius plot

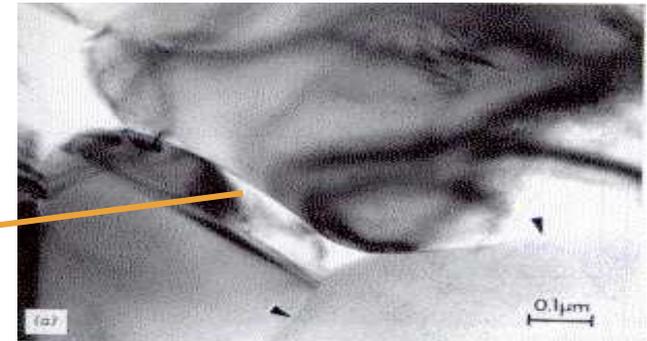
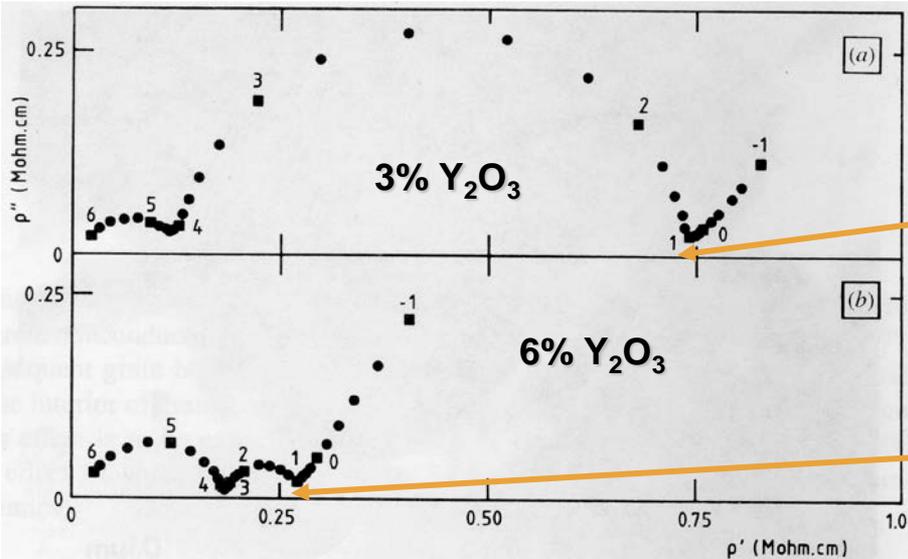
$$\square = \square_0 \exp(E_{\square}/kT)$$

E_{\square}
↗ bulk
↘ g.b.

- ✓ Evaluation of E_{\square}
- ✓ Properties of the grain boundary
- ✓ Comparison of $E_{a_{\text{gb}}}$ and $E_{a_{\text{bulk}}}$
- ✓ Conclusions for structure & conductivity mechanisms



➤ Conductivity characterization: bulk; grain boundaries

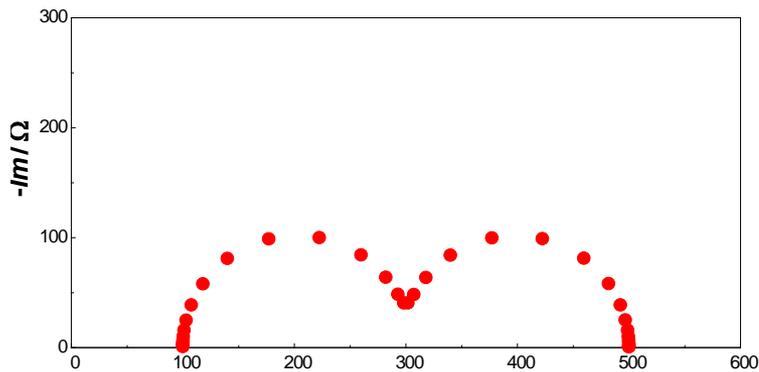


Zirconia ceramics: Impedance Spectroscopy, Emphasizing Solid Materials and Systems, ed. J.R. Macdonald, 1987, p.219

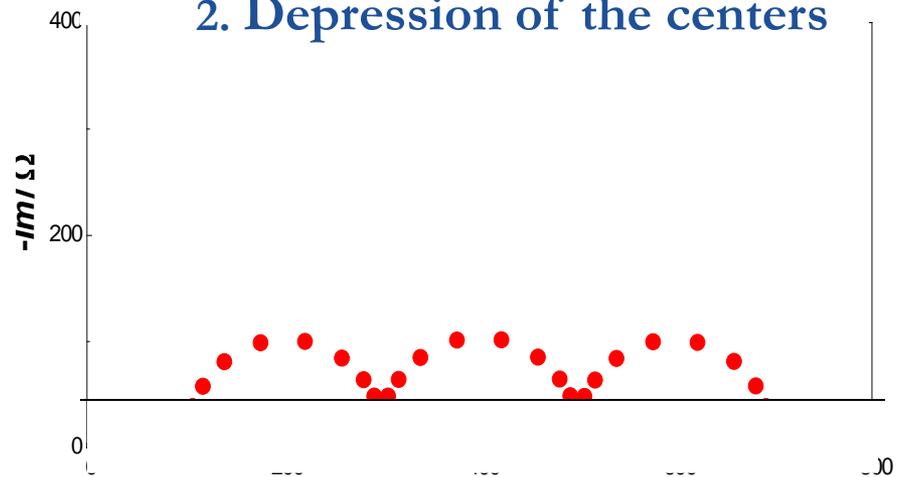


➤ **Deviations** in real systems from the Idealized Model

1. High degree of mixing of T



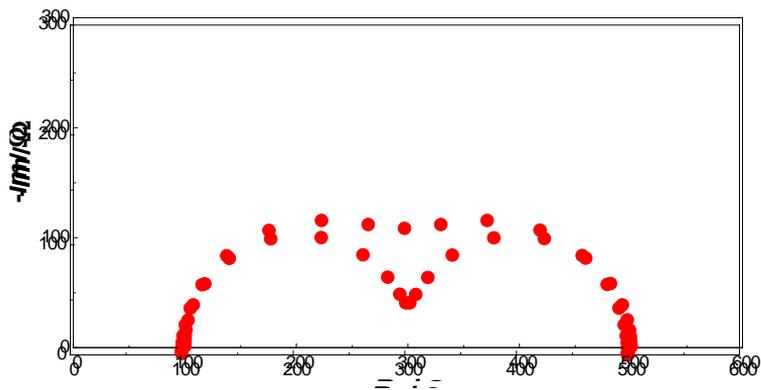
2. Depression of the centers



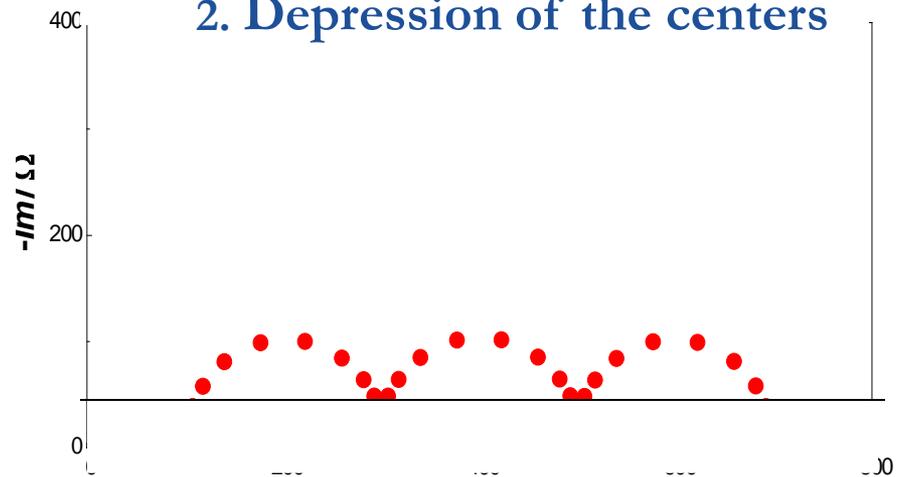


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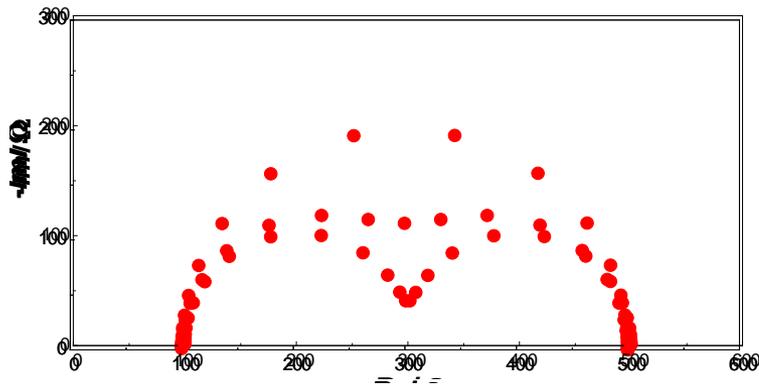
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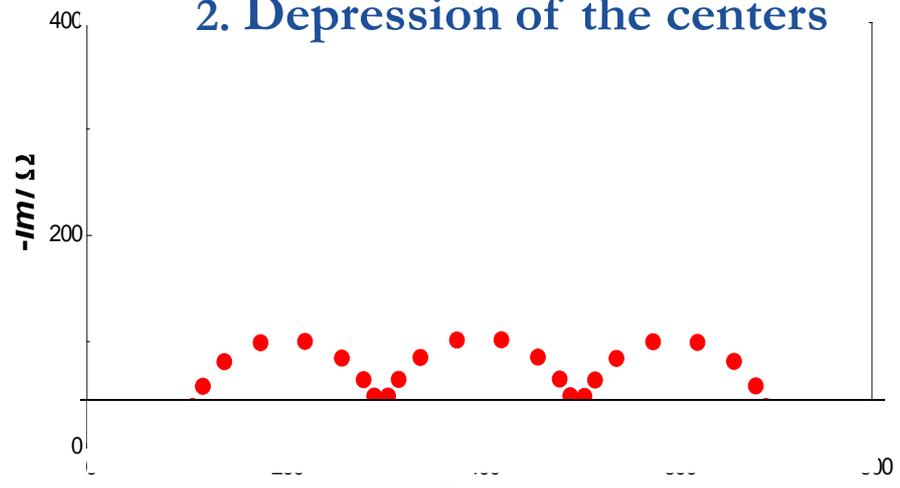


➤ **Deviations** in real systems from the Idealized Model

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2. Depression of the centers

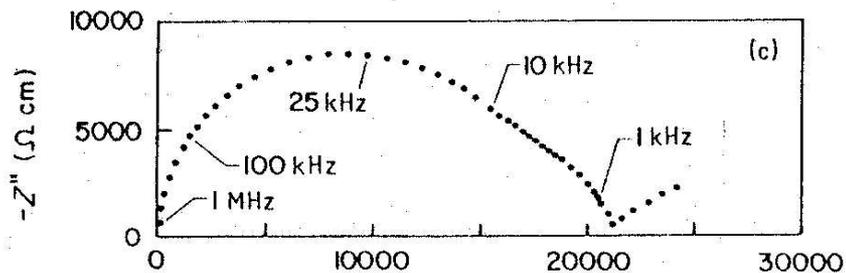




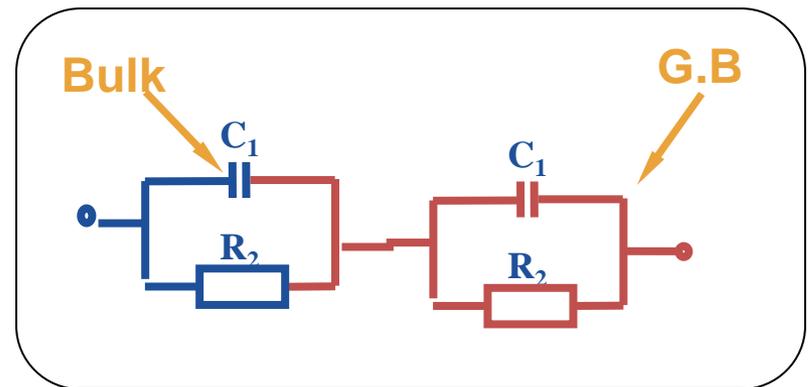
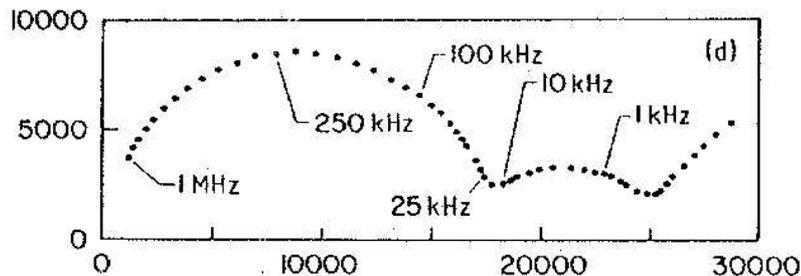
➤ Real Samples Impedance – MORE COMPLICATED

- ✓ BULK - second phase (including pores); vacancy ordered structures; magnetic or electric domains;
- ✓ G.B. – accumulation or depletion of space charge; impurities; defects; second phase;

YSZ – clean grain boundaries



YSZ grain boundaries with impurities

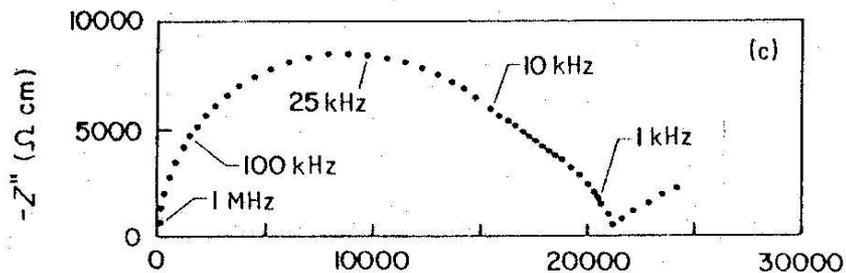




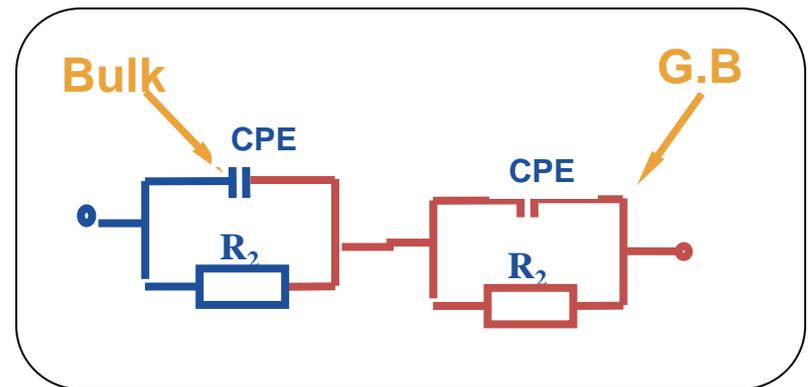
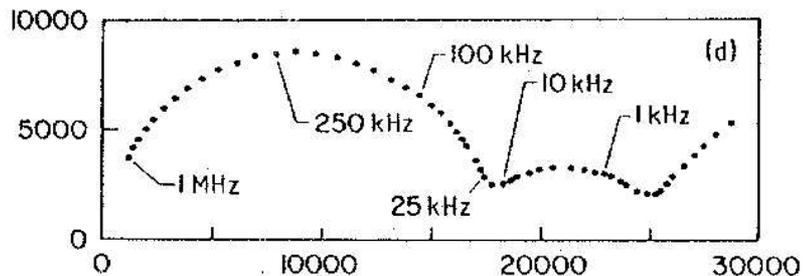
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YSZ grain boundaries with impurities





➤ Basic (idealized) Model - interpretation

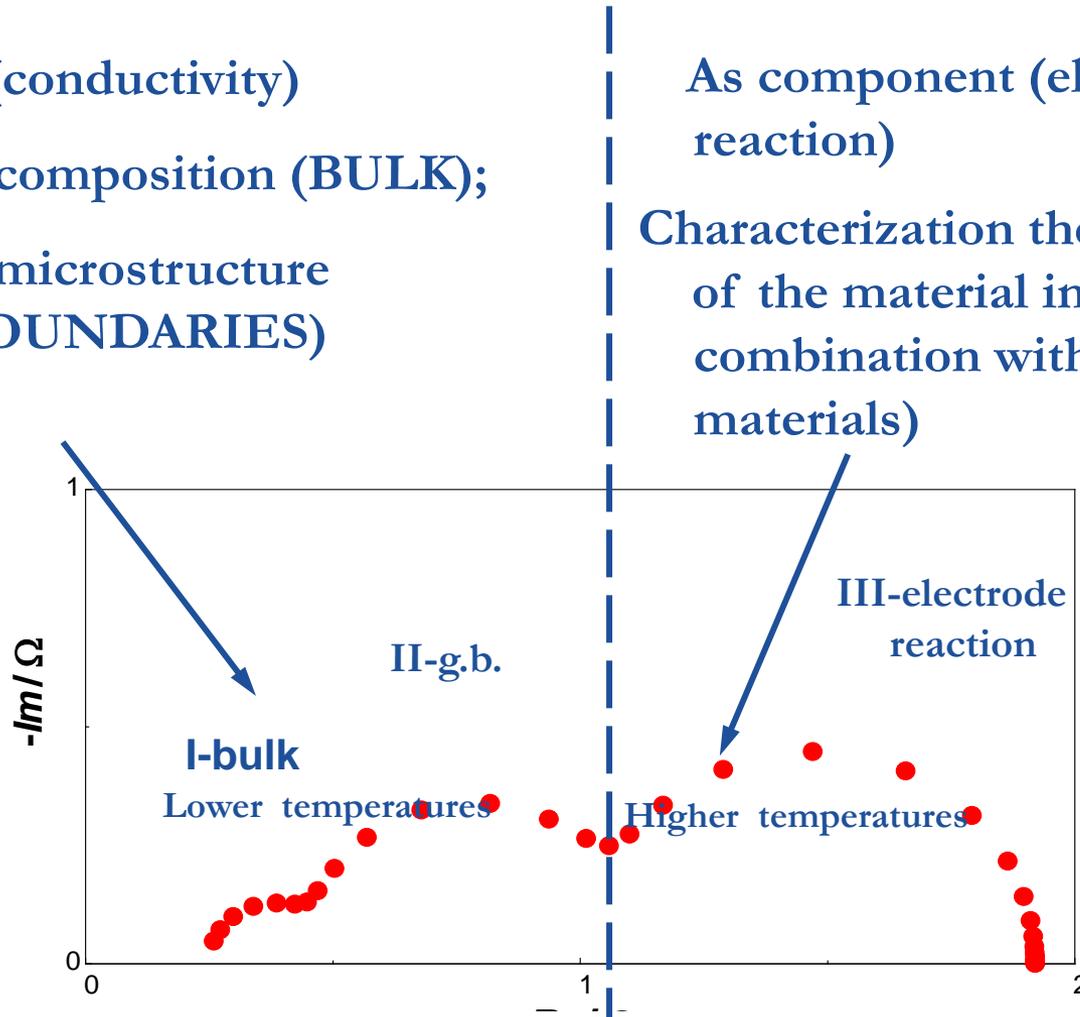
As Material (conductivity)

Influence of composition (BULK);

Influence of microstructure
(GRAIN BOUNDARIES)

As component (electrode
reaction)

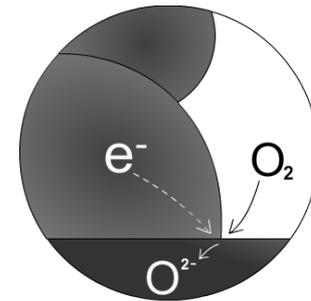
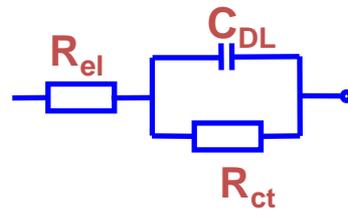
Characterization the functionality
of the material in a process (in
combination with other
materials)





➤ Electrode reaction description

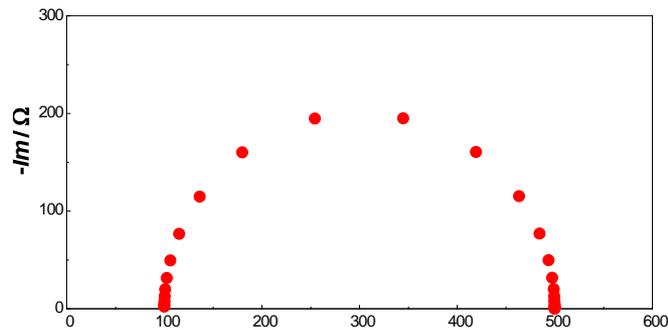
✓ Charge transfer approach (adopted from liquid Electrochemistry – idealized description)



✓ Assumption:

Electrochemical (charge transfer) reaction takes place at the three phase boundary (metal-electrolyte-gas)

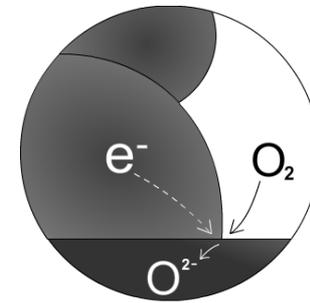
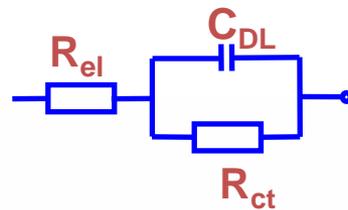
Idealized model





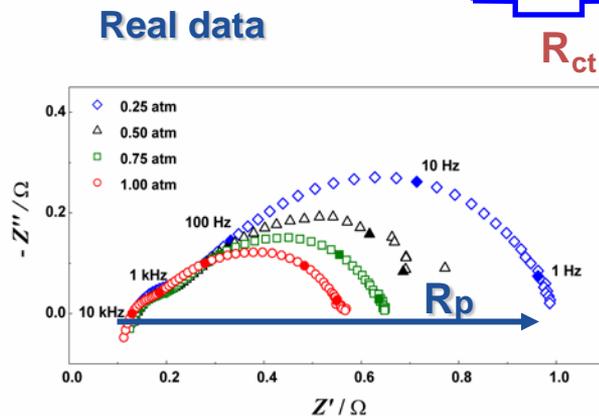
➤ Electrode reaction description

✓ Charge transfer approach (adopted from liquid Electrochemistry – idealized description



✓ Assumption:

- Electrochemical (charge transfer) reaction takes place at the three phase boundary (metal-electrolyte-gas)
- Break down of the electrode reactions on individual steps involving : 2 D charge transfer, different diffusions, adsorption etc.



P. Carpanese, A. Barbucci, G. Cerisola et al,
Bulg. Chem. Communic. 38 (2006) 186





SUMMARY (1)

What can impedance give for SOFC studies

- **Materials and components:**
 - Electrolyte: R_b , $R_{g,b}$, optimization of microstructure
 - Electrodes: polarization resistance R_p , quality of interface, rate limiting stage, quality of deposition;
- **Cells:** performance; separation of components influence, influence of water behaviour; gas flow, temperature



SUMMARY (2)

What else can impedance give :

- PLEASURE and
- RELAXATION

Mattice: Dance 1

Impedance: Ferri-ferrocyanide System



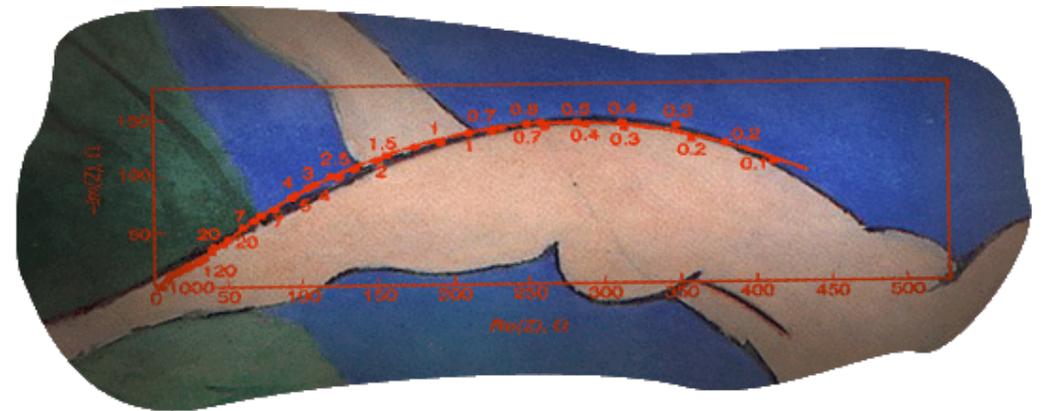
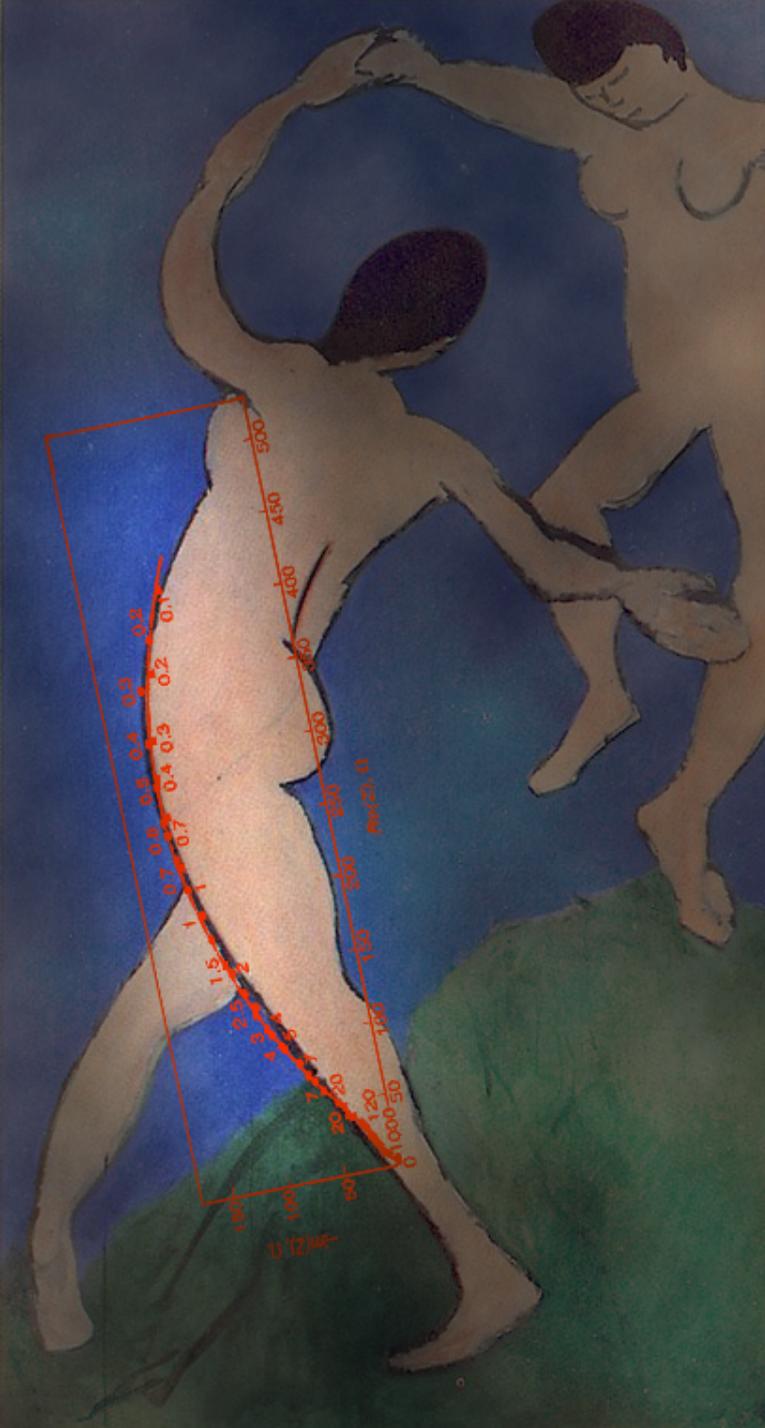
Mattice: Dance 1

Impedance: Ferri-ferrocyanide System



Mattice: Dance 1

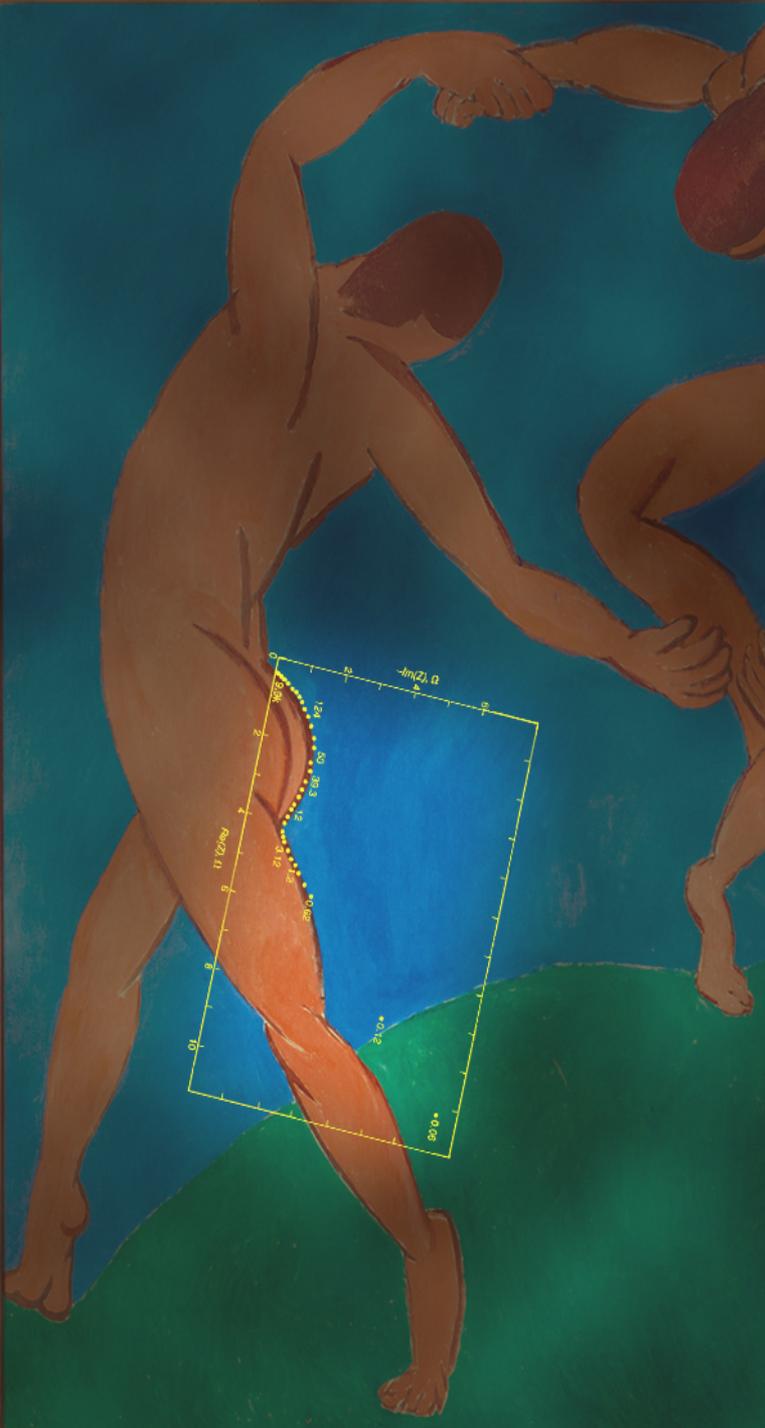
Impedance: Ferri-ferrocyanide System





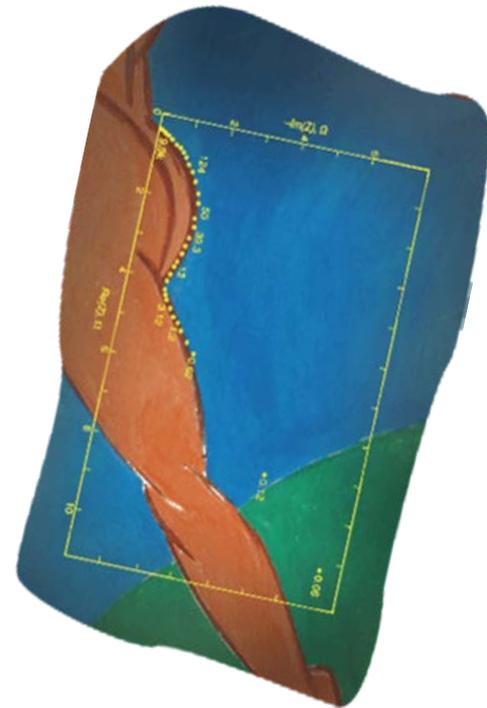
Mattice: Dance 2

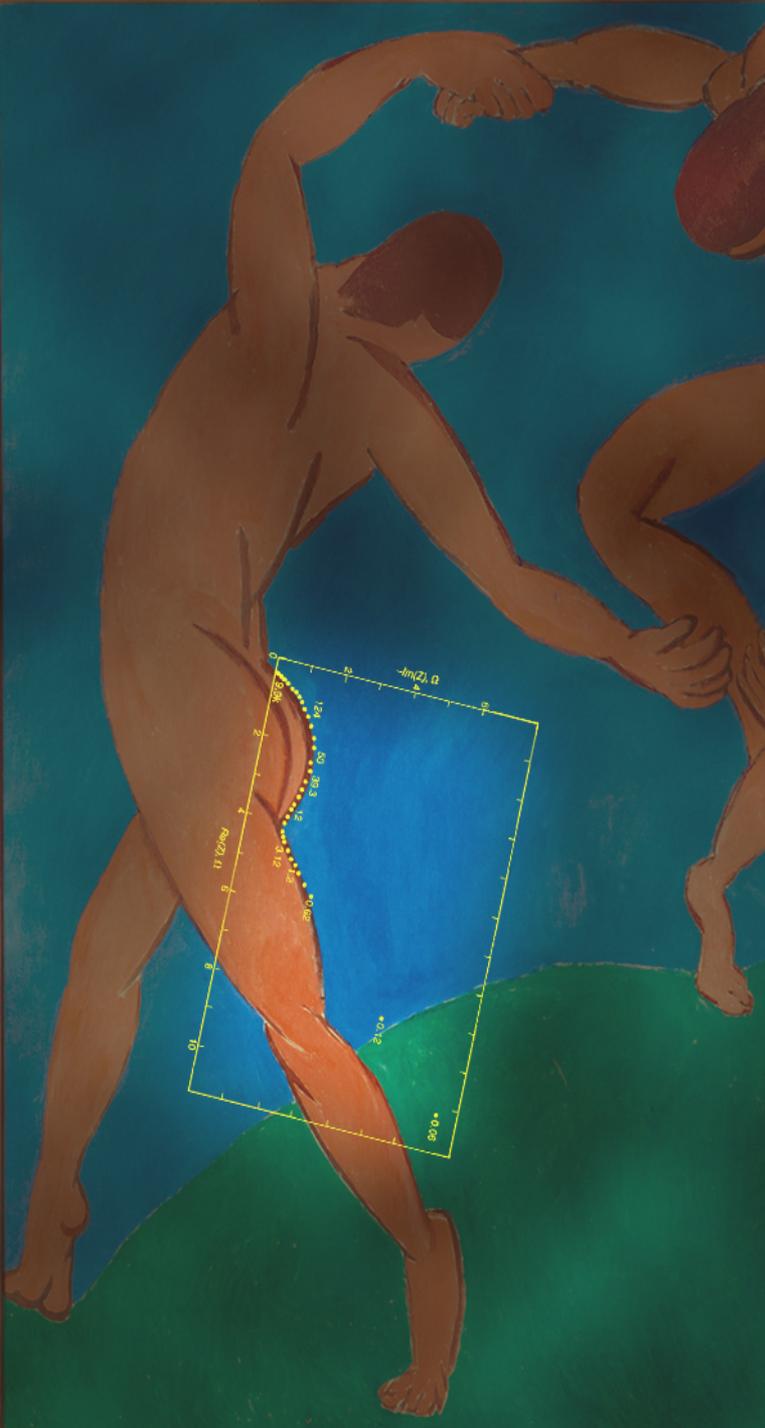
Impedance: Armico iron/organic coating



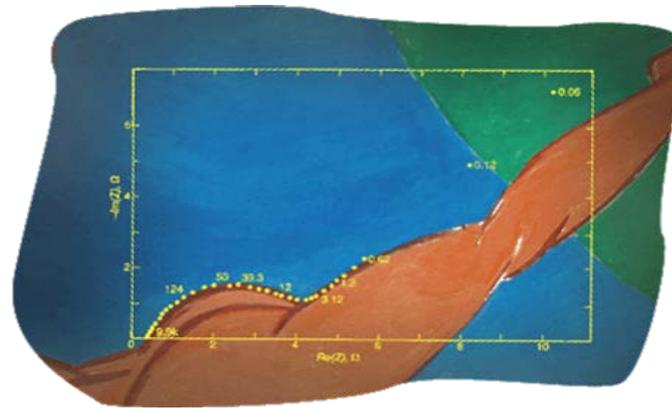
Mattice: Dance 2

Impedance: Armico iron/organic coating





Mattice: Dance 2
Impedance: Armico iron/organic coating





ACKNOWLEDGEMENTS

INSTITUTE OF ELECTROCHEMISTRY AND ENERGY SYSTEMS ACADEMICIAN EVGENI BUDEVSKI



The e - course was prepared in the frames of the project:

“conductivity and reversibility Mechanisms in an Innovative design of solid oxide fuel cell” - IMOOD ;

“Изследване Механизмите на проводимост и Обратимост в иновативен Дизайн на твърдооксидна горивна клетка” - ИМООД

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